

Kinetic Biochemistry

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Abstract: Mathematics and computer programming have a major contribution to chemistry. Two directions can be identified: one that searches and tries (rich) to explain the structural binding and shape of the chemical compounds [1] with major applications in QSPR/QSAR studies [2], and applied sciences such as engineering of materials or agriculture [3]; the second direction is to models the kinetic processes that are involved in chemical reactions [4]. Many such models are available here. The present paper describes three variants of well the known kinetic models and presents the mathematical equations associated with them. The differential equations are numerically solved and fitted with MathCad program.

Keywords: numerical methods, kinetics, oscillating reactions

Introduction

The oscillating reactions are the most spectacular and essential for life [5]. All live processes are based on one or more oscillating reactions [6,7].

The possibility of periodically altering the concentrations of the reactants, the agents and the product, in space and time, is a result of the autocatalysis. Fig. 1 represents two temporary aspects of the space distribution (distribution in space) of the reaction products through the concentration wave front in the proximity of the electron participates in the reaction as a reactant.

The oscillating reactions are more than a laboratory curiosity [8,9]. If in the industrial processes they appear in few cases, in biochemical systems there are numerous examples of oscillating reactions [10,11]. For instance, the oscillating reactions maintain the rhythm [12,13].

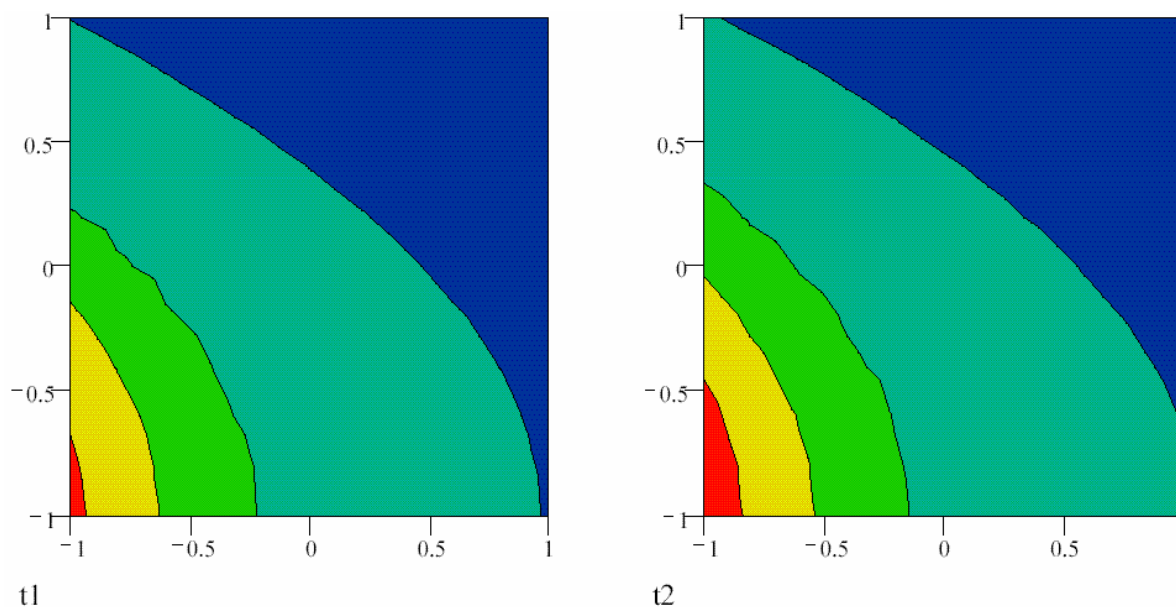


Fig. 1. Concentration gradient in an oscillating reaction at the t , and at the $t + \Delta t$ moments;

Avi animation: <http://lori.academicdirect.ro/free/RO.avi>

A general characteristic of the oscillating reactions is that, under the same conditions, all the participants from the reaction chain oscillate with the same frequency but a different displacement (lagging) shift.

1. Diffusion

In case of liquid phase, reactant particles must pass through solvent particles and collisions of reactants are not frequent such in gases, the mobility of them is much lower [14]. From this reason, the collision time is bigger and in this time interval of molecules contact appear the probability that the system of molecules to accumulate enough energy to react. The molecules of reactant are permanently surrounded by solvent molecules and must be considered the entire energy of local assembly. More, the molecules of solvent can active participate to reaction as intermediary catalyst of process [15, 16]. In conclusion, the global

reaction process in liquids is more complex than gases [17, 18]. Anyway, it can be decomposed in simple processes through establishing of a kinetic scheme [19,20].

Let a reaction through two reactants, R_1 and R_2 and let κ_d be the forming constant of R_1R_2 compound. The reaction process is expressed by:



Forming of R_1R_2 is determined by diffusion characteristics of R_1 and R_2 . Assuming that the reaction (1) has a spherical symmetry, the diffusion equation of property ϕ in space (r) and time (t) are expressed by:

$$\frac{\partial \phi(r, t)}{\partial t} = K \cdot \left(\frac{\partial^2 \phi(r, t)}{\partial r^2} + \frac{2}{r} \cdot \frac{\partial \phi(r, t)}{\partial r} \right) \quad (2)$$

If R_2 diffuses through R_1 , then R_1 are in the center of coordinate reference and if diffusing property ϕ is R_2 concentration $[R_2]$, then (2) become:

$$\frac{\partial [R_2]}{\partial t} = K \cdot \left(\frac{\partial^2 [R_2]}{\partial r^2} + \frac{2}{r} \cdot \frac{\partial [R_2]}{\partial r} \right) \quad (3)$$

Reducing the diffusion process to the stationary case, (3) are annulling:

$$\frac{\partial [R_2]}{\partial t} = 0 = K \cdot \left(\frac{\partial^2 [R_2]}{\partial r^2} + \frac{2}{r} \cdot \frac{\partial [R_2]}{\partial r} \right) \quad (4)$$

To solve and fit the concentration gradient of R_2 a second order differential equation must be solved:

$$\frac{d^2 [R_2]}{dr^2} + \frac{2}{r} \cdot \frac{d [R_2]}{dr} = 0 \quad (5)$$

The equation (5) has two constants after integration, which it result from limit conditions. For simplifying, let us note:

$$\frac{d [R_2]}{dr} = r^2 \quad (6)$$

With (6), the equation (5) becomes:

$$\frac{dr^2}{dr} + \frac{2}{r} \cdot r^2 = 0 \quad (7)$$

By multiplying of (7) with dr/r^2 , it becomes a simple differential equation:

$$\frac{1}{r^2} \cdot dr^2 + \frac{2}{r} \cdot dr = 0 \quad (8)$$

The equation (8) can be integrated member by member, when it results:

$$\ln(r_2) + 2\ln(r) = a \Rightarrow r_2 \cdot r^2 = a \Rightarrow r_2 = \frac{a}{r^2} \quad (9)$$

where a is a integration constant. Using again (6) the resulted equation (9) becomes:

$$d[R_2] = \frac{a}{r^2} dr \quad (10)$$

By integration of (10), it result expression of $[R_2]$ depending on radius r :

$$[R_2] = b - \frac{a}{r} \quad (11)$$

The value of a , and b parameters are determined from:

$$b = [R_2](\infty) = [R_2]_\infty \text{ and } [R_2](r_0) = 0 \quad (12)$$

where first equality express the fact that at huge distance from R_1 molecules, where R_2 concentration is observed one from mass of solution, $[R_2]_0$, and the second equality express the fact that there exist r_0 coordinate from R_1 molecules where concentration of R_2 are null through reaction of R_1 and R_2 . More, r_0 is the coordinate at which molecules are close enough to react. The reaction is not instant, such as we can believe. This phenomenon is explained by fact that the relation (11) does not contain the temporal coordinate, t .

Expressing the relations (11) and (12) through the entire space ($r > 0$) we obtain:

$$\frac{[R_2]}{[R_2]_\infty} = \begin{cases} 0, & r < r_0 \\ 1 - r_0/r, & r \geq r_0 \end{cases} \quad (13)$$

equation that are fitted in following graph:

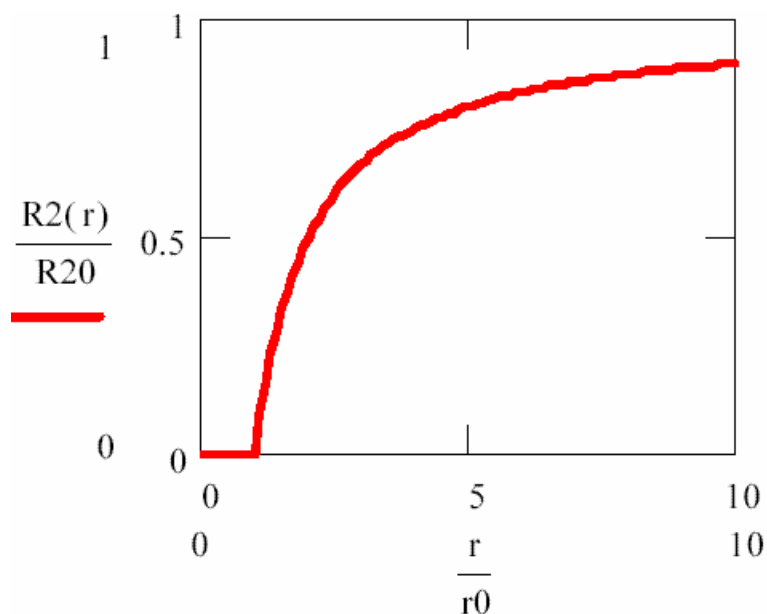


Fig. 2. Variation of R_2 in vicinity of R_1 molecules (diffusion and reaction phenomena)

The radial flux of [R2] is:

$$J_{R_2} = -D_{R_2} \frac{d[R_2]}{dr} = \begin{cases} 0, & r < r_0 \\ [R_2]_{\infty} \cdot r_0 / r^2, & r \geq r_0 \end{cases} \quad (14)$$

and at coordinate of reaction the radial flux is:

$$J_{R_2}(r_0) = [R_2]_{\infty} / r_0 \quad (15)$$

The mean value of concentration that crosses the surface $4 \cdot \pi \cdot r_0^2$ in a one unit of time (the variation of concentration in time, rate of concentration variation through surface) is:

$$[\dot{R}_2](r_0) = -4\pi r_0 D_{R_2} [R_2]_{\infty} \quad (16)$$

Reaction rate of R_2 with molecules of R_1 , noted with u_{21} are obtained multiplying this quantity (expressed by 16) with number of R_1 molecules from one unity of volume (with $[R_1]_0 \cdot N_A$):

$$u_{21} = -4\pi r_0 D_{R_2} [R_2]_{\infty} [R_1]_{\infty} N_A \quad (17)$$

Repeating these calculations for hypothesis of R_1 molecules diffusion through field of R_2 molecules, it results:

$$u_{12} = -4\pi r_0 D_{R_1} [R_2]_{\infty} [R_1]_{\infty} N_A \quad (18)$$

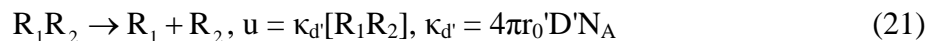
Real rate of reaction u are a mean value of these theoretical results obtained through model simplifying in hypothesis that R_2 diffuse to R_1 and respectively R_1 diffuse to R_2 . In reality, these phenomena are present simultaneously and competitive:

$$u = (u_{12} + u_{21})/2 = -4\pi r_0 D [R_2]_{\infty} [R_1]_{\infty} N_A, \quad D = (D_{R_1} + D_{R_2})/2 \quad (19)$$

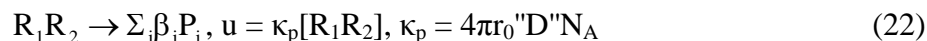
The minus sign in expression of rate u is because of reference system choosing, the diffusion is from big positive values of r to small positive values of them. The values $[R_2]_{\infty}$ and $[R_1]_{\infty}$ are concentrations recorded in mass of solution (more exactly [R1] and [R2]) it result the value of rate constant for a reaction controlled by diffusion in spherical symmetry:

$$\kappa_d = 4\pi r_0 D N_A \quad (20)$$

The pair $R_1 R_2$ can also to dissociate through a process without reaction, so:



or can form reaction products (different from R_1 and R_2):



Let us come back to hypothesis of stationary (time independence). Mass of reaction is constant in most of time, such that the $[R_1R_2]$ concentration of pairs is ready to consume and to form products or to become again reactants. Expressing this fact, we can write:

$$u_{R_1R_2} = u_{R_1R_2 \text{ from eq(1)}} - u_{R_1R_2 \text{ from eq(21)}} - u_{R_1R_2 \text{ from eq(22)}} = 0 \quad (23)$$

and, replacing the expressions of $u_{R_1R_2}$:

$$\kappa_d[R_1][R_2] = (\kappa_{d'} + \kappa_p) \cdot [R_1R_2], [R_1R_2] = \frac{\kappa_d}{\kappa_{d'} + \kappa_p} [R_1][R_2] \quad (24)$$

The equation (22) is only one that contains also the rate of products forming. Using (22) and (24), it results:

$$u_j = \beta_j \kappa_p [R_1][R_2] = \beta_j \frac{\kappa_p \kappa_d}{\kappa_p + \kappa_{d'}} [R_1][R_2] \quad (25)$$

The equation (25) has two limit cases. When $\kappa_{d'} \ll \kappa_p$ the equation (25) becomes:

$$u_j = \beta_j \kappa_p [R_1][R_2] = \beta_j \kappa_d [R_1][R_2] \quad (26)$$

and the reaction are controlled in exclusivity by diffusive capacity of reactants. When $\kappa_p \ll \kappa_{d'}$ the equation (25) becomes:

$$u_j = \beta_j \kappa_p [R_1][R_2] = \beta_j (\kappa_d \kappa_p / \kappa_{d'}) [R_1][R_2] \quad (27)$$

where are easy to observe that $\kappa_d / \kappa_{d'}$ is equilibrium constant of the reaction:



and in this case the diffusive control disappear (see expressions of κ_d and $\kappa_{d'}$) and the reaction are controlled kinetically and the transformation into products are make with energy consuming from environment (the energy are accumulate in collision pair from surrounding molecules of solvent).

2. Mass Balance in Controlled by Diffusion Reactions

The general equation of diffusion can be written in Cartesian coordinates:

$$\dot{\phi}(x,y,z,t) = K \Delta \phi(x,y,z,t) - \vec{V} \cdot (\vec{i} + \vec{j} + \vec{k}) \phi(x,y,z,t) v(x,y,z,t) \quad (29)$$

where is assumed that diffusion are joined also by convection, which is transport of property makes through solvent movement. The equation (29) are established based on diffusion and convection phenomena in a space region $((x,y,z),(x+dx,y+dy,z+dz))$ without considering a

possible reaction that can decrease or increase the value of ϕ property in considered space region. A reaction is possible and is generally independent of space coordinates. Expressing his dependence, we can write:

$$\dot{\phi}(x,y,z,t) = \kappa \phi^{\gamma_{\phi}} \quad (30)$$

where γ_{ϕ} is reaction order. Completing the equation (29) with the term from (30), it results:

$$\dot{\phi}(x,y,z,t) = K\Delta \phi(x,y,z,t) - \vec{\nabla} \cdot (\vec{i} + \vec{j} + \vec{k}) \phi(x,y,z,t)v(x,y,z,t) + \kappa \phi^{\gamma_{\phi}} \quad (31)$$

The equation (31) named the equation of mass balance for the property ϕ and is applied in numerous chemical processes. Two such examples are the diffusion of oxygen in blood and the diffusion of a gas to the surface of a catalyst [21, 22]. The solutions of (31) equation are not easy to obtain. The equation is a inhomogeneous differential one. The analytical solving is possible only in few special cases. For projecting of chemical reactors and kinetic biochemistry analysis that use this equation, are makes through numerical methods based on a specific real model of reaction [23].

Expressing the equation (31) in one-dimensional case without convection and with a property consume of 1 reaction order ($\gamma_{\phi} = 1$), it result:

$$\dot{\phi}(x,t) = K \phi_x''(x,t) + \kappa \phi(x,t) \quad (32)$$

If a function $Q(x,t)$ is a solution of equation without reaction, then:

$$\dot{Q}(x,t) = K Q_x''(x,t) \quad (33)$$

and $\phi(x,t)$ are given by:

$$\phi(x,t) = Q(x,t)e^{\kappa t} \quad (34)$$

is a solution of equation with reaction (equation 32).

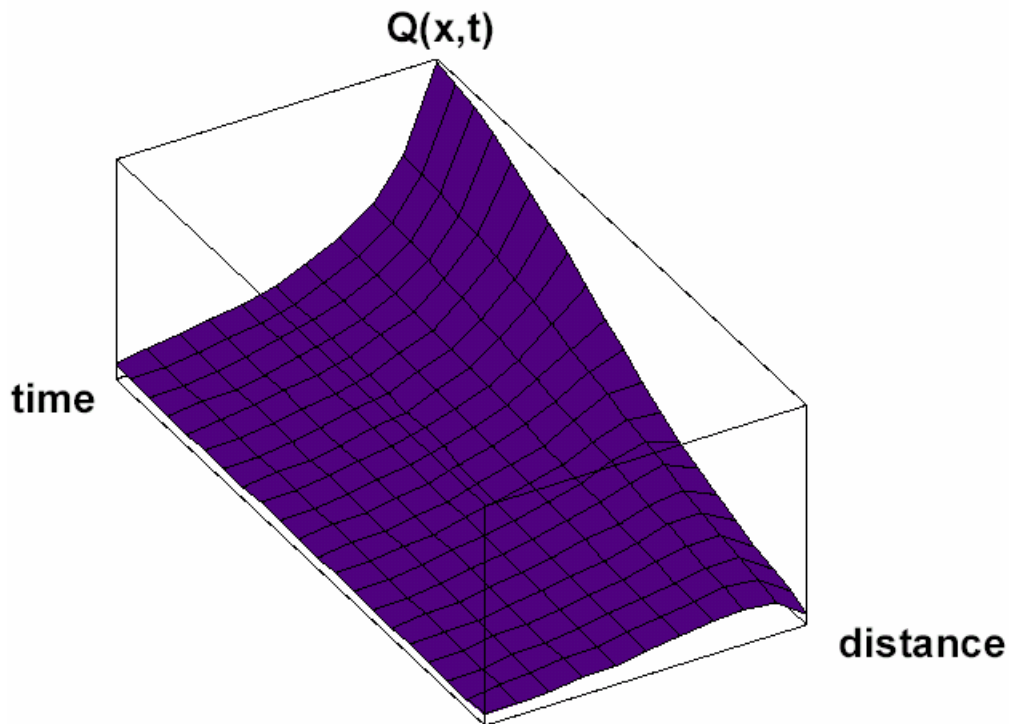
About the equation (33) and his solution, it is completely solved using distribution theory [24]. The general solution of (33) in \mathfrak{R}^n space ($x = (x_1, \dots, x_n)$) is:

$$Q(x_1, \dots, x_n, t) = \frac{1}{(\sqrt{4K\pi t})^n} e^{-\frac{(x_1^2 + \dots + x_n^2)}{4Kt}} \quad (35)$$

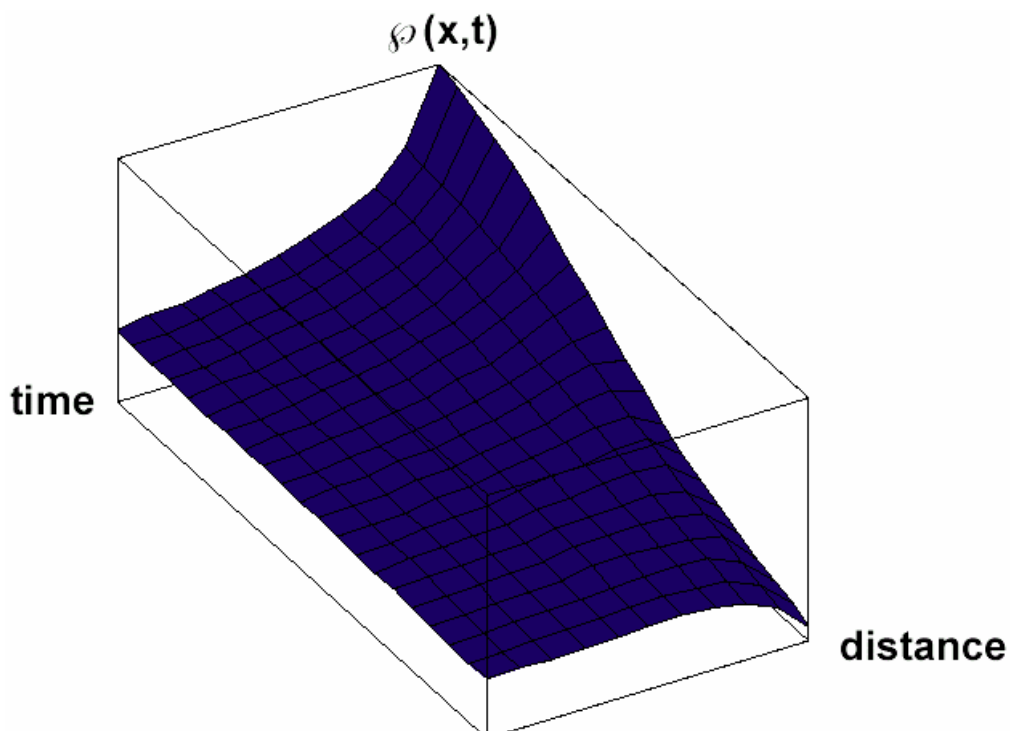
For $n = 1$ (\mathfrak{R}^1) we obtain the solution of equation (33). Replacing in (34) this solution, it results:

$$Q(x, t) = \frac{1}{\sqrt{4K\pi t}} e^{-\frac{x^2}{4Kt}} e^{-\kappa t} \quad (36)$$

Particular solutions of these equations are plotted in figs. 3-5.



*Fig. 3. Space and time dependence of property ϱ with diffusion:
solution $Q(x,t)$ of (33) for $K = 2$*



*Fig. 4. Space and time dependence of property ϱ with diffusion and property forming
($\kappa > 0$ in equation 32) solution $\varphi(x,t)$ of (32) for $K = 2$ and $\kappa = 3$*

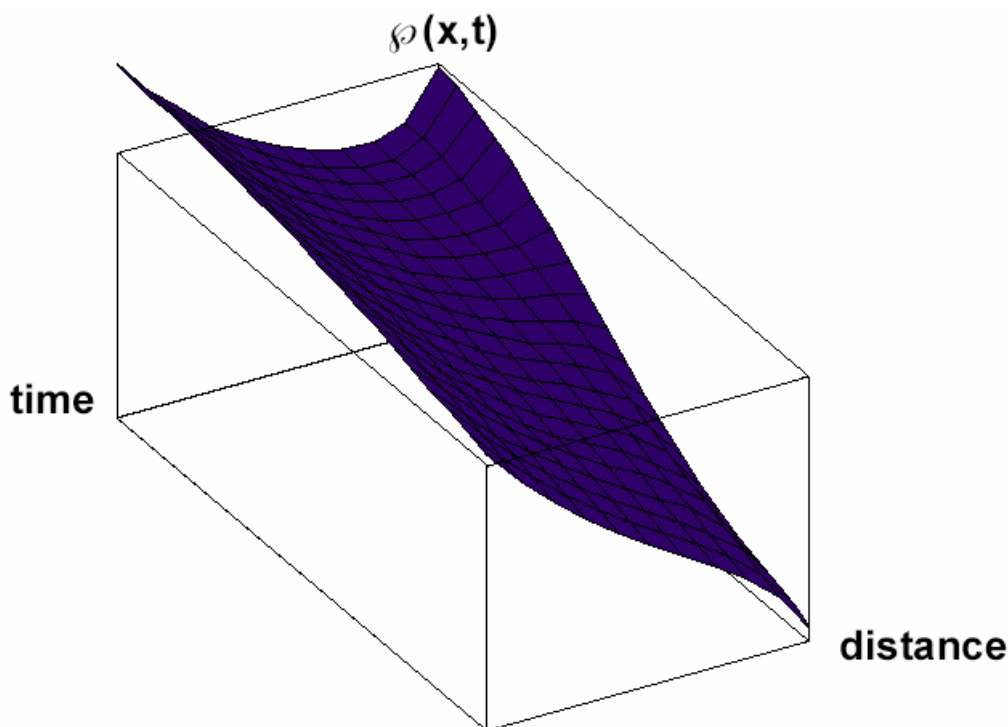
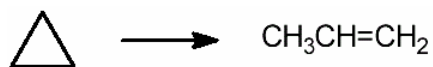


Fig. 5. Space and time dependence of property ϕ with diffusion and property consuming ($\kappa < 0$ in equation 32) solution $\phi(x,t)$ of (32) for $K = 2$ and $\kappa = -3$

3. Monomolecular Reactions

In a monomolecular reaction a single molecule go through a structure rearrangement or decomposition [25]. Such process is rearrangement of cyclopropane to propene:



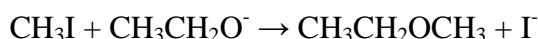
The general case of monomolecular reaction is governed by the equation:



The rate law for such a reaction is written directly based on chemical equation of reaction. Rearrangement of propene has, according to (37) a single product of reaction, so $J = 1$ and $\beta_j = 1$. A monomolecular reaction is of order 1 because molecules number from reactant which are decomposing in a short time interval are directly proportional with number of molecules available to react, so with $[\text{R}]$.

4. Bimolecular Reactions

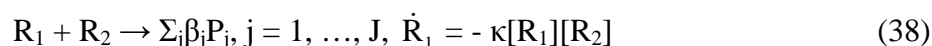
In such a reaction have collision and exchange energy two molecules, atoms or group of atoms. Note that the implied species can make also other exchanges (such as electrons). Bimolecular reaction is also the equations of following type, between methyl iodide and ethylic alcohol in alcohol medium:



The mechanism of this reaction is bimolecular, proved by experimental rate law:

$$v = \kappa[\text{CH}_3\text{I}][\text{CH}_3\text{CH}_2\text{O}^-]$$

Generally,



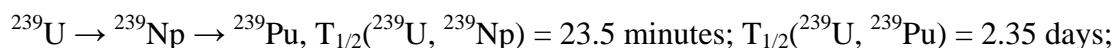
A bimolecular reaction is of order 2 because his rate is proportionally with speed of reactants in moment of collision, so with his concentrations.

Any assumption related to the mechanism of a reaction, including the reactions of order 2 mechanisms, must be followed by testing phase of assumed model.

Note that the correspondence between order of a reaction and reaction type is not a bi-univocal one. Thus, if reaction is an elementary process of second order, then the order of reaction is two. Reverse, if order of reaction is two, reaction may be following a complex mechanism. The postulated mechanism can be augmented through investigation of secondary products and intermediaries.

5. Monomolecular Consecutive Reactions

Another elementary case is for monomolecular consecutive reactions [26,27], such as radioactive fission [28,29]:



The general case is expressed by:



Let $\kappa_{1,2}, \dots, \kappa_{n-1,n}$ be the rate constants of monomolecular processes $\text{R}_i \rightarrow \text{R}_{i+1}$. Then, the decomposition rate of R_1 is given by:

$$\dot{\text{R}}_1 = -\kappa_{1,2}[\text{R}_1] \quad (40)$$

and global rates of R_2, \dots, R_{n-1} intermediaries forming are given by the differences between rate of his forming reaction and rate of his decomposing reaction [30]:

$$\dot{R}_j = -\kappa_{j,j+1}[R_j] + \kappa_{j-1,j}[R_{j-1}], j = 2, \dots, n-1 \quad (41)$$

Forming rate of final product R_n is given by an expression similarly to (40):

$$\dot{R}_n = \kappa_{n-1,n}[R_{n-1}] \quad (42)$$

Integration of (40) lead to:

$$[R_1] = [R_1]_0 e^{-\kappa_{1,2}t} \quad (43)$$

If are assumed that initially only R_1 are present ($[R_j]_0 = 0, j > 1$), then the (41) equations solutions can be obtained successively and the first integration lead to:

$$[R_2] = \frac{\kappa_{1,2}}{\kappa_{2,3} - \kappa_{1,2}} (e^{-\kappa_{1,2}t} - e^{-\kappa_{2,3}t}) [R_1]_0 \quad (44)$$

Is complicate to go on with formal solving of differential equations system (41), replacing of (44) in (41) conduct us at inhomogeneous differential equation of order 1, but can be solved elegantly using a formal or numeric specialized software. The identifying of the integration constants that appear at solving steps is makes with respect to initial values of concentrations (in our case $[R_j]_0 = 0$ for $j > 0$) and the equation of concentration balance:

$$[R_1] + [R_2] + \dots + [R_n] = [R_1]_0 + [R_2]_0 + \dots + [R_n]_0 \quad (45)$$

In particular case taken from literature [31] of $n = 3$ and $[R_2]_0 = [R_3]_0 = 0$, the expression of $[R_3]$ is:

$$[R_3] = \left(1 - \frac{\kappa_{2,3} e^{-\kappa_{1,2}t} - \kappa_{1,2} e^{-\kappa_{2,3}t}}{\kappa_{2,3} - \kappa_{1,2}}\right) [R_1]_0 \quad (46)$$

and in figure 6, are depicted the dependencies in this particular case.

The point of maximum for R_2 concentration is obtaining from annulling first order derivate of concentration:

$$\begin{aligned} \dot{[R_2]} &= [R_1]_0 \frac{\kappa_{1,2}}{\kappa_{2,3} - \kappa_{1,2}} (\kappa_{2,3} e^{-\kappa_{2,3}t} - \kappa_{1,2} e^{-\kappa_{1,2}t}) = 0, \\ \kappa_{1,2} / \kappa_{1,2} &= e^{(\kappa_{1,2} - \kappa_{2,3})t}, \quad t_{2,\max} = \frac{\ln(\kappa_{1,2}) - \ln(\kappa_{2,3})}{\kappa_{1,2} - \kappa_{2,3}} \end{aligned} \quad (47)$$

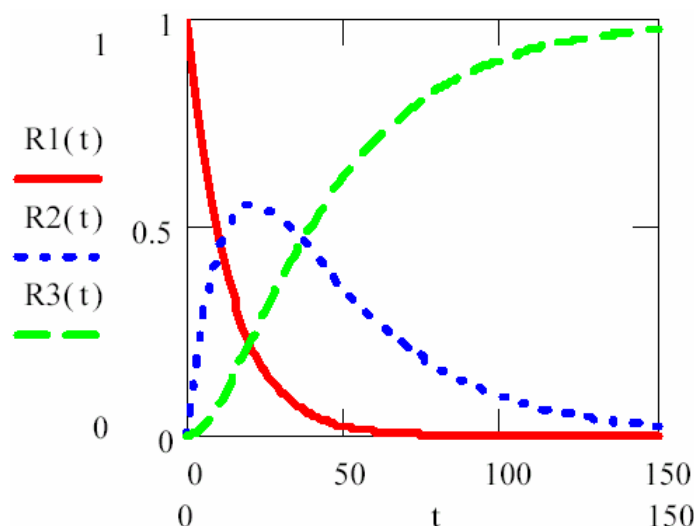


Fig. 6. Concentrations variations for three consecutive monomolecular reactions

with $[R_1]_0 = 1 \text{ mol}\cdot\text{l}^{-1}$, $[R_2]_0 = [R_3]_0 = 0 \text{ mol}\cdot\text{l}^{-1}$, $\kappa_{1,2} = 3/40$, $\kappa_{2,3} = 2/71$

The equations system:

$$\begin{cases} t_{2,\max} = \frac{\ln(\kappa_{1,2}) - \ln(\kappa_{2,3})}{\kappa_{1,2} - \kappa_{2,3}} \\ [R_2]_{\max} = [R_1]_0 \frac{\kappa_{1,2}}{\kappa_{2,3} - \kappa_{1,2}} (\kappa_{2,3} e^{-\kappa_{2,3} t_{2,\max}} - \kappa_{1,2} e^{-\kappa_{1,2} t_{2,\max}}) \end{cases} \quad (48)$$

are very useful in practice, when are measured the time $t_{2,\max}$ and the concentration $[R_2]_{\max}$ and after that are identified the values of rate constants $\kappa_{1,2}$ and $\kappa_{2,3}$.

If we start from (46) with substitution $K = \kappa_{2,3}/\kappa_{1,2}$ and proper grouping of terms it result:

$$[R_3]/[R_1]_0 = 1 - \frac{\kappa_{2,3} e^{-\kappa_{1,2} t} - \kappa_{1,2} e^{-\kappa_{2,3} t}}{\kappa_{2,3} - \kappa_{1,2}} = 1 - e^{-\kappa_{1,2} t} \left(1 + \frac{1 - e^{-\kappa_{1,2} t (K-1)}}{K-1} \right) \quad (49)$$

The equation (49) expresses a dependency of $[R_3]/[R_1]_0$ by time and K for a choused decomposing reaction $R_1 > R_2$ and a 3D dependency was plotted in fig. 7.

For $K < 1$ ($\kappa_{2,3} < \kappa_{1,2}$) the determining rate stage is first stage ($R_1 > R_2$) until the time rich the value of 104 s. In this time interval (0-104 s) with high priority are accumulating the R_2 intermediary and after that, in short time, R_2 are transformed to R_3 .

For $K > 1$ ($\kappa_{2,3} > \kappa_{1,2}$) the determining rate stage is second stage ($R_2 > R_3$) it was in fact the responsible for surface shape for $\lg(\kappa_{2,3}/\kappa_{1,2}) + 5 > 5$.

The figure 7 proves that in a process that evolve through consecutive reactions, for rate constant significant different there exist always a stage that determinate reaction rate, and these is the stage that evolve with lowest rate.

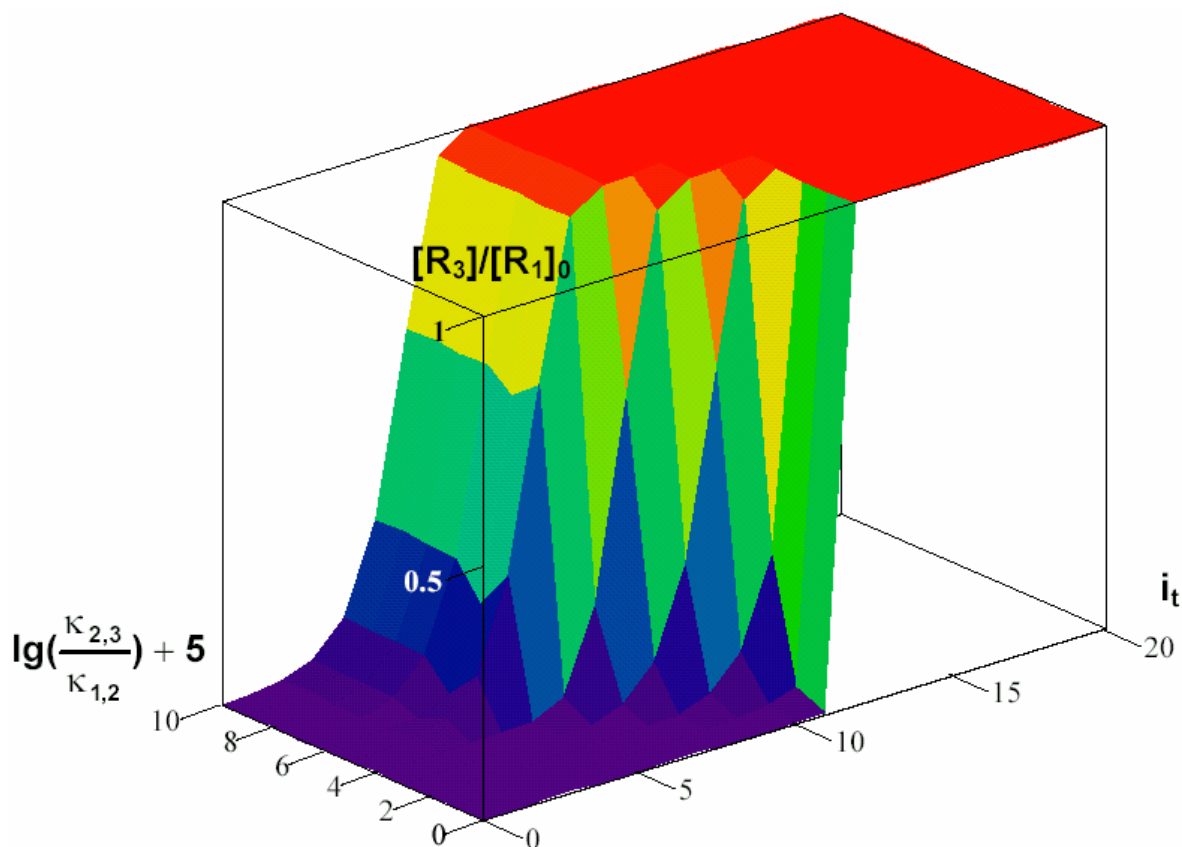


Fig. 7. Surface of R_3 forming depending on forming rate (expressed by $\kappa_{2,3}/\kappa_{1,2}$ value) and time (expressed by i_t value) for $\kappa_{1,2} = 1/2$ and $t = 10^{i_t/2-1} - 1$, $i_t = 0, \dots, 20$, $K = \kappa_{2,3}/\kappa_{1,2} = 10^{j-5}$, $j = 0, \dots, 10$

6. Pre-equilibrium

The case of chemical reactions that evolve governed by equation:



will be discussed in this section.

The equation (50) implies a pre-equilibrium, the state in which a intermediary (R_3) are in equilibrium with the reactants [32, 33]. Pre-equilibrium appear practically when the

forming rate of intermediary and decomposing rate of them into reactants are much higher than products forming rate [34]:

$$\kappa_1, \kappa_2 \gg \kappa_3 \quad (51)$$

If (51) are true, it can be considered that R_1 , R_2 and R_3 are in equilibrium and:

$$[R_3]/([R_1][R_2]) = \kappa_1/\kappa_2 = K \quad (52)$$

From following equation, the forming rate of R_4 can be determined:

$$[\dot{R}_4] = \kappa_3[R_3] = \kappa_3K[R_1][R_2] \quad (53)$$

The (53) equation type is a second order one with rate constant κ given by:

$$\kappa = \kappa_3K = \kappa_3\kappa_1/\kappa_2 \quad (54)$$

If we don't ignore the fact that $R_3 > R_4$ is a slow reaction, we can use the approximation of stationary phase on R_3 :

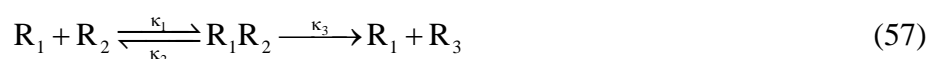
$$\dot{R}_3 = \kappa_1[R_1][R_2] - \kappa_2[R_3] - \kappa_3[R_3] = 0 \quad (55)$$

and reaction rate will be:

$$\dot{R}_4 = \kappa_3[R_3] = \kappa[R_1][R_2], \quad \kappa = \frac{\kappa_1\kappa_3}{\kappa_2 + \kappa_3} \quad (56)$$

7. Michaelis – Menten Mechanism

Michaelis – Menten mechanism work with respect to the equation [35]:



and are frequently applied at enzymatic catalysis (where R_1 are enzyme, R_2 are substrate and R_3 it cumulate the obtained products after enzyme action [36,37]).

The rate of enzymatic catalyzed reaction [38] depends on enzyme concentration $[R_1]$ even if the enzyme do not go through a net change (are achieve in reaction products, [39]). If we follow the same judgment of stationary phase (equation 55):

$$\frac{d[R_1R_2]}{dt} = \kappa_1[R_1][R_2] - \kappa_2[R_1R_2] - \kappa_3[R_1R_2] \quad (58)$$

From (58) it result the expression of $[R_1R_2]$:

$$[R_1][R_2] = \frac{\kappa_1}{\kappa_2 + \kappa_3} [R_1][R_2] \quad (59)$$

Concentration balance is:

$$[R_1]_0 = [R_1] + [R_1R_2] \quad (60)$$

If we substitute $[R_1]$ from (60) into (59), it results:

$$[R_1R_2] = \frac{\kappa_1}{\kappa_2 + \kappa_3} [R_2]([R_1]_0 - [R_1R_2]) \quad (61)$$

From (61) $[R_1R_2]$ can be extracted. Then result:

$$[R_1R_2] = \frac{\kappa_1}{\kappa_1[R_2] + \kappa_2 + \kappa_3} [R_1]_0[R_2] \quad (62)$$

Forming rate of R_3 (like equation 56) is:

$$[\dot{R}_3] = \kappa_3[R_1R_2] = \frac{\kappa_3}{[R_2] + \frac{\kappa_2 + \kappa_3}{\kappa_1}} [R_2][R_1]_0 \quad (63)$$

The K_M are named Michaelis constant and are given by:

$$K_M = \frac{\kappa_2 + \kappa_3}{\kappa_1} \quad (64)$$

Using (63) and (64) the general expression of R_3 forming rate (hardly used in enzymatic catalysis) is:

$$[\dot{R}_3] = \kappa[R_1]_0, \quad \kappa = \frac{\kappa_3[R_2]}{K_M + [R_2]} \quad (65)$$

To express the dependency of κ constant by $[R_2]$ substrate concentration, the following equation is useful:

$$\kappa = \frac{\kappa_3}{1 + K_M/[R_2]} \quad (66)$$

κ 's dependency of $[R_2]/K_M$ value are fitted in fig. 8.

Usually, the enzyme quantity is much lower than substrate quantity, so we have:

$$[R_2] \gg [R_1R_2], [R_2] \approx [R_0] \quad (67)$$

The (67) equation it correspond to horizontal portion of dependency from fig. 8 and describe most of the enzymatic process evolution (until the vicinity of final point). If (67) are replaced in (65), it results:

$$[\dot{R}_3] = \kappa[R_1]_0, \quad \kappa = \frac{\kappa_3[R_2]_0}{K_M + [R_2]_0} \quad (68)$$

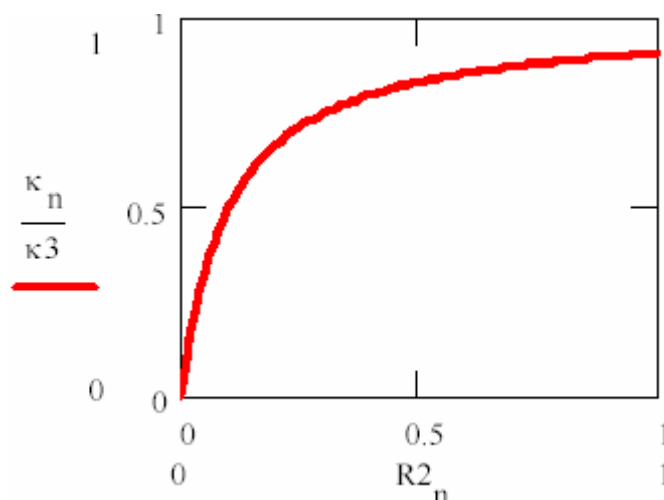


Fig. 8. Rate constant (κ) in Michaelis – Menten mechanism (n are iteration number)

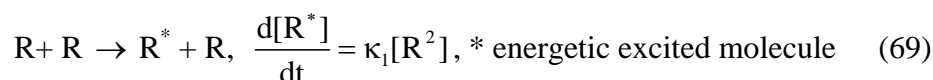
The Michaelis - Menten mechanism are also successfully applied to inorganic reactions [40].

8. Lindemann – Hinshelwood Mechanism

Chemical processes evolve in reality in a much complex mode than can be expressed through the mechanisms presented until now. These are only approximations, and have serious difficulties and limitations when we want a deeper study of reactions mechanism [41,42]. A prove of this fact are the studies initiated by Lindemann and completed by Hinshelwood for case of monomolecular reactions. Them proposed model, that assume that reactant molecule require activation to pass into products are depicted in fig. 9.

The mechanism consists in:

1. collision of two fast molecules R:



2. collision of a energetic excited molecule R^* with unexcited one:



3. transformation of energetic excited molecule into products:



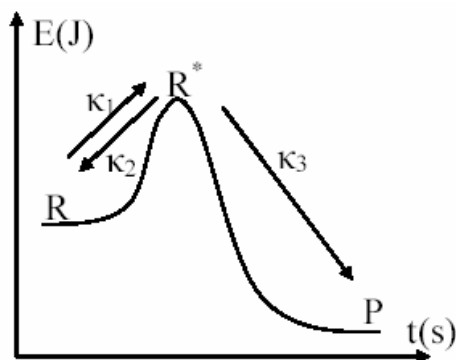


Fig. 9. Energetic activation in Lindemann – Hinshelwood Mechanism

From experimental observations, which show that global reaction has a kinetic of order 1, such as we presented through (37) equation, it result that the main rate phase (slowest one) is third one ($\kappa_3 < \kappa_1, \kappa_2$). At same result are done if stationary phase approximation for R^* is applied:

$$\frac{d[R^*]}{dt} = \kappa_1[R^*]^2 - \kappa_2[R^*][R] - \kappa_3[R^*] = 0 \Rightarrow [R^*] = \frac{\kappa_1[R]^2}{\kappa_3 + \kappa_2[R]} \quad (72)$$

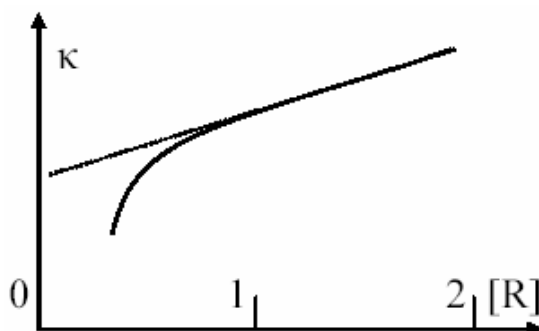


Fig. 10. Linearity approximation in monomolecular processes vs. L–H Mechanism

Rate equation is:

$$\frac{d[P]}{dt} = \kappa_3[R^*] = \frac{\kappa_3\kappa_1[R]^2}{\kappa_3 + \kappa_2[R]} = \kappa[R], \text{ where } \kappa = \frac{\kappa_3\kappa_1[R]}{\kappa_3 + \kappa_1[R]} \quad (73)$$

At limit, when $\kappa_3 \ll \kappa_2[R]$ and κ_3 are ignored in relation to $\kappa_2[R]$, the (37) equation is obtained, according to the simplified model of monomolecular processes. Dependence of κ constant by reactant concentration is depicted in fig. 10.

The Lindemann – Hinshelwood model are capable to explain the changing of reaction order for monomolecular reactions when $[R]$ concentration is lower [43], but does not provide a detailed explanation of real processes. κ 's dependence curvature is even more significant in

reality for very low concentrations of $[R]$ then predicted curvature from second order kinetic reaction. An adjusting of this model was makes by Rice, Ramsperger and Kassel [44], which replace the third stage ($R^* \rightarrow P$) with:



where R^* is the molecule with high energy and R^\dagger is activated molecule. They introduce a rate constant for every stage. This construction has explanation that the accumulated energy is distributed to all bonds from molecule. It result that exist a delay in transition of R^* to products, provoked by previous forming of activated molecule R^\dagger ($R^* \rightarrow R^\dagger$).

Using the differential equation system:

$$\begin{cases} d[P] = \kappa_4[R^\dagger]dt \\ d[R^\dagger] = (\kappa_3[R^*] - \kappa_4[R^\dagger])dt \\ d[R^*] = (\kappa_1[R]^2 - \kappa_2[R^*] - \kappa_3[R^*])dt \\ d[R] = (\kappa_2[R][R^*] - \kappa_1[R]^2)dt \end{cases} \quad (75)$$

obtained based on equations (69), (70) and (74) a graphical dependences of reactant $[R]$, product $[P]$ and intermediaries $[R^*]$, $[R^\dagger]$ was plotted in fig. 11 and 12 for rate constants $\kappa_1 = 0.2$, $\kappa_2 = 0.1$, $\kappa_3 = 0.9$ and $\kappa_4 = 0.5$ with initial concentration of R $[R] = x_0 = 1$ and time interval $t_n = 0, \dots, 30$.

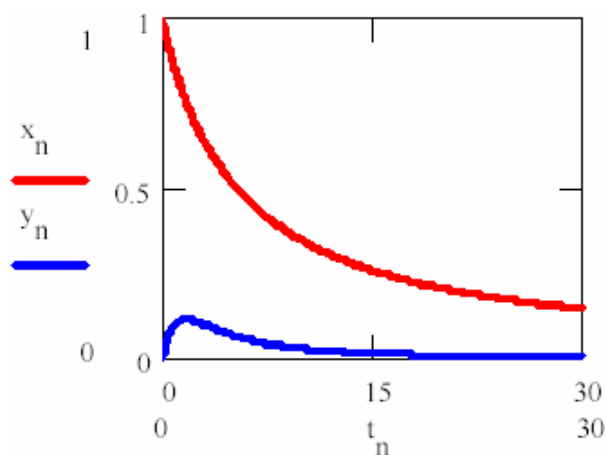


Fig. 11. Concentration – time dependence for reactant R (x_n on graph) and R^* (y_n on graph), eq. 75

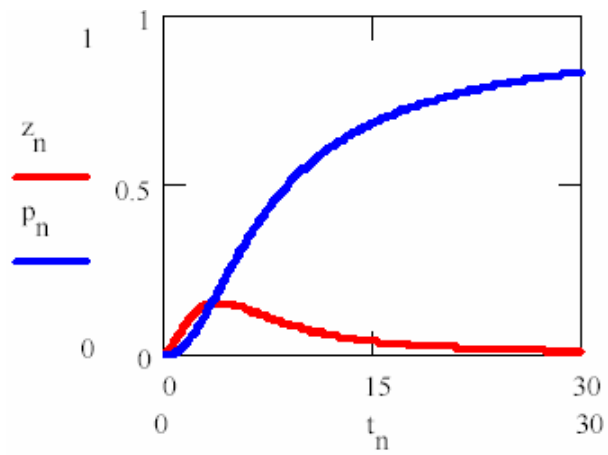


Fig. 12. Concentration – time dependence for product P (p_n on graph) and R^\dagger (z_n on graph), eq. 75

9. Catalyzed Processes

If activation energy of a reaction is big, only a small ratio of molecular collisions produces reaction. The catalysts has role to decrease the activation energy of the reaction by providing another way to pass to products, that avoid the slow rate stage of reaction and lead to a increased rate of reaction, at same temperature [45,46].

Here an example of catalyzed reaction: activation energy for H_2O_2 decomposing in solution is $76\text{kJ}\cdot\text{mol}^{-1}$ and the reaction is slow at room temperature. If we add iodine in small quantities, the activation energy decrease at $57\text{kJ}\cdot\text{mol}^{-1}$ and the reaction rate grows about 2000 times [47].

Enzymes are biological catalyst. It is very specific and can have a spectacular effect on his controlled reactions. The activation energy for acid hydrolysis of sucrose is of $107\text{kJ}\cdot\text{mol}^{-1}$. In presence of sucrase enzyme, the energy is decreased to $36\text{kJ}\cdot\text{mol}^{-1}$ and hydrolysis process is accelerated about 10^{12} times at body temperature (310 K).

A homogenous catalyst is in same phase with reaction mixture. Exist also heterogenous catalysts (placed somewhere else than reaction mixture) such as a solid catalyst for a gas phase reaction [48,49].

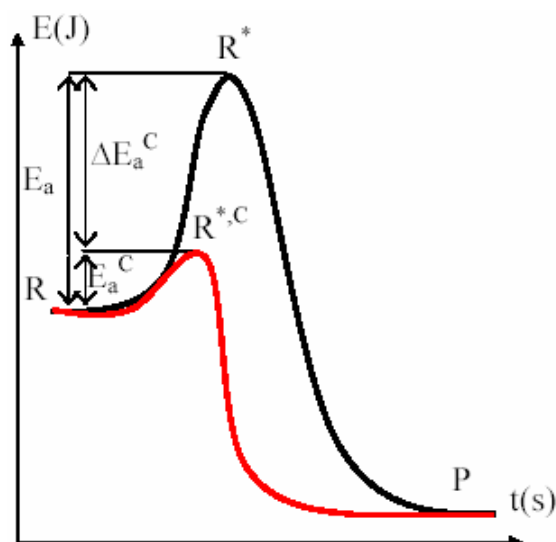


Fig. 13. Energetic tunneling with catalysts

The fig. 13 presents the corridor tunneling from reactants to products by using catalyst. The most important cases of homogenous catalysis are base catalysis and acid catalysis. They are implied frequently organic reactions, each one or both. The easiest action

mode of them is through Brönsted mechanism. Therefore, Brönsted acid catalysis consists in a proton transfer to the S substrate from a HA acid:

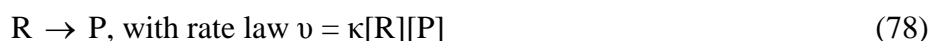


This process is primary one in ester solvolysis [50,51] keto-enolic tautomerism and sucrose inversion [52,53]. Brönsted base catalysis consists in a proton transfer from S substrate to B base:



This process is primary one in isomerisation and halogenation of organic compounds, and at Claisen and aldolc reactions [54, 55].

Autocatalysis phenomena consists in acceleration of a reaction makes by his products [56, 57]. An example of autocatalysed reaction is:



In equation (78) the reaction rate is increased together with reaction products formation. Expressing the variation of product concentration, it results:

$$v = \frac{d[P]}{dt} = \kappa[R][P] = \kappa([R]_0 + [P]_0 - [P])[P] \quad (79)$$

By integration of the (79) equation we obtain:

$$C = \frac{1}{[R]_0 + [P]_0} \ln \frac{[P]}{[R]_0 + [P]_0 - [P]} - \kappa t \quad (80)$$

where C is obtained from initial conditions. Resolving the initial conditions in (80):

$$\ln \frac{[P]_0}{[R]_0} = \ln \frac{[P]}{[R]_0 + [P]_0 - [P]} - \kappa([R]_0 + [P]_0)t \quad (81)$$

or:

$$\frac{[P]}{[R]_0 + [P]_0 - [P]} = \frac{[P]_0}{[R]_0} e^{\kappa([R]_0 + [P]_0)t} \quad (82)$$

and:

$$[P] \left(1 + \frac{[P]_0}{[R]_0} e^{\kappa([R]_0 + [P]_0)t} \right) = ([R]_0 + [P]_0) \frac{[P]_0}{[R]_0} e^{\kappa([R]_0 + [P]_0)t} \quad (83)$$

The (83) equation allows us to express the [P] concentration depending only by time and initial conditions:

$$[P] = [P]_0 \frac{[R]_0 + [P]_0}{[R]_0 e^{-\kappa([R]_0 + [P]_0)t} + [P]_0} \quad (84)$$

The (84) equation are plotted in fig. 14, for $[P]_0 = 0.1$, $[R]_0 = 0.99$, $\kappa = 4$:

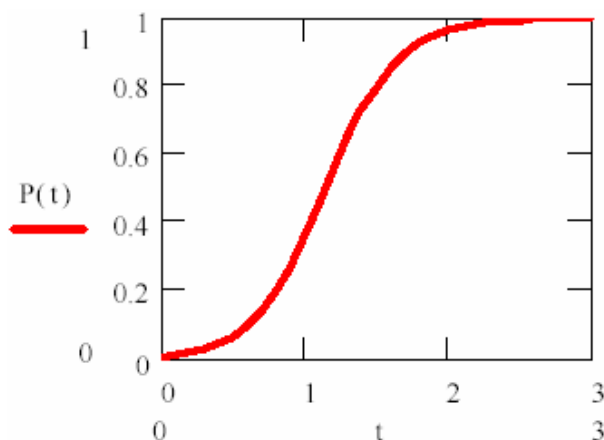


Fig. 14. Variation of product concentration in an autocatalysed reaction

The reaction rate is obtained from (84) equation differentiating or through (84) substitution into (79).

It can be observed that the reaction rate is small at beginning and increase together with P product forming until his maximum value (for $[P] = [R]$). After that, it has decrease, such as can be observed in fig. 15.

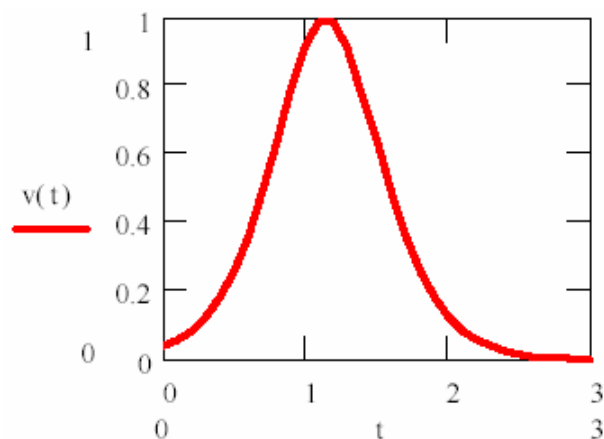


Fig. 15. Product's concentration variation rate into a autocatalysed reaction

If we are interested to find the time moment when the reaction rate is maximum, the following equation are useful:

$$t_{\max} = \frac{\ln \frac{[R]_0}{[P]_0}}{\kappa([R]_0 + [P]_0)} \quad (85)$$

The industrial importance of autocatalysis is significant [58]. Therefore, autocatalysis appears in oxidation reactions, when autocatalysis study allow to maximize the reaction rate through continue assuring of optimal concentrations of reactant and product. This is the field of automated industrial processes.

10. Explosions

Rapid increasing of rate constant by temperature provokes a thermo explosion [59,60]. If the reaction is exothermic one, and provoke increasing of reaction environment increasing then acceleration of reaction rate it has as result a much faster increasing of both temperature and reaction rate [61]. To exemplifying, let us assume that temperature is linear increased by products concentration (then decrease proportionally with reactant concentration) and rate constant is increased with temperature through Arrhenius law:

$$T = T_0 - \alpha[R], \quad \alpha > 0, \quad \kappa = Ae^{-\beta T}, \quad \beta > 0 \quad (86)$$

If we express the κ constant by $[R]$:

$$\kappa = Ae^{-\beta(T_0 - \alpha[R])} = Ae^{-\beta T_0} e^{\alpha\beta[R]} = \kappa_0 e^{\alpha\beta[R]} \quad (87)$$

and assume that the reaction is first order one by concentration:

$$[\dot{R}] = -\kappa[R] \quad (88)$$

we can replace the κ value from (87):

$$[\dot{R}] = -\kappa_0 e^{\alpha\beta[R]} [R] \quad (89)$$

Separating now the variables:

$$0 = \kappa_0 e^{\alpha\beta[R]} [R]^{-1} d[R] + \kappa_0 dt \quad (90)$$

By integration of (90) it results:

$$t = \frac{\int_{[R]}^{[R_0]} x^{-1} e^{-\alpha\beta x} dx}{\kappa_0} \quad (91)$$

which is a $t = t([R])$ dependency.

By fitting this dependency (fig. 16) and reversing it, the $[R] = [R](t)$ dependency is obtained:

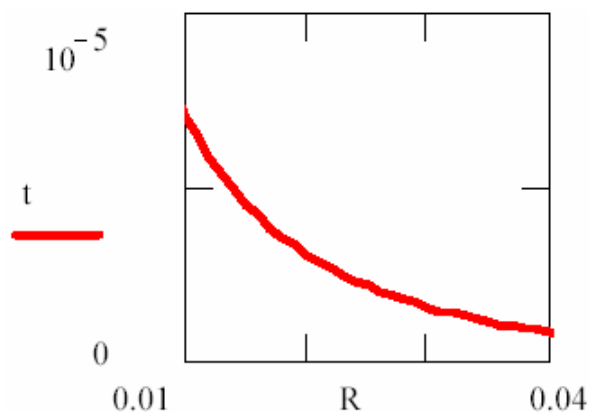


Fig. 16. Explosion phenomena, $t = t([R])$ diagram

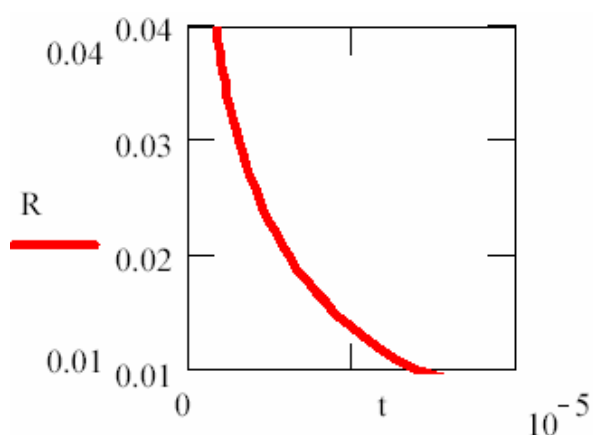


Fig. 17. Explosion phenomena, $[R] = [R](t)$ diagram

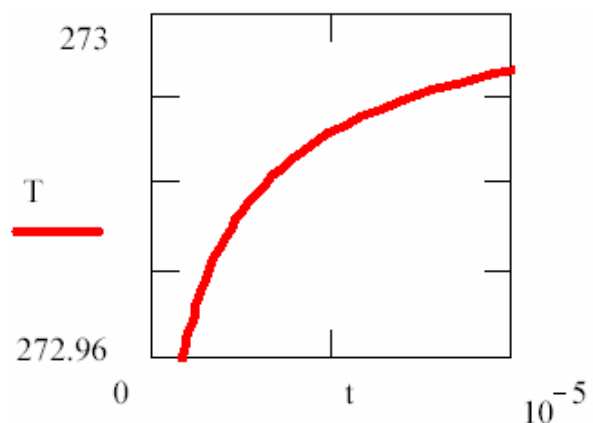


Fig. 18. Explosion phenomena, $T = T(t)$ diagram

Using the (86) relation, we can also plot the $T = T(t)$ dependency (fig. 18). The explosion phenomena are explained by fact that the slope of $[R] = [R](t)$ and $T = T(t)$ curves are vertically in $t = 0$ (17 and 18 figures). Consuming of most of $[R]$ reactant quantity, such as we can observe on graphs, fitted for $\alpha = 1$, $\beta = 40$, $\kappa = 105$, it correspond to a short time.

The final point of explosion has, of course, $[R] = [R](t)$ and $T = T(t)$ null curves slope.

The experimental study of explosion that are produced when oxygen and hydrogen react:



allowing to establish the following mechanism:

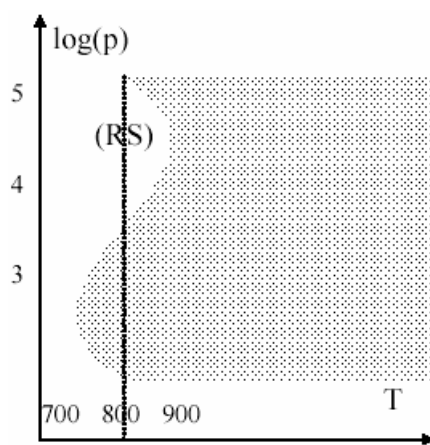
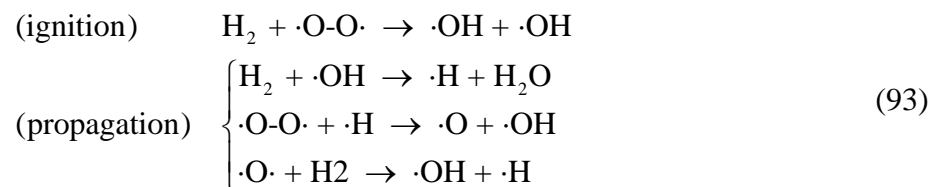


Fig. 19. $\text{H}_2 + \text{O}_2$ explosion

Other secondary reaction was identified, such as:

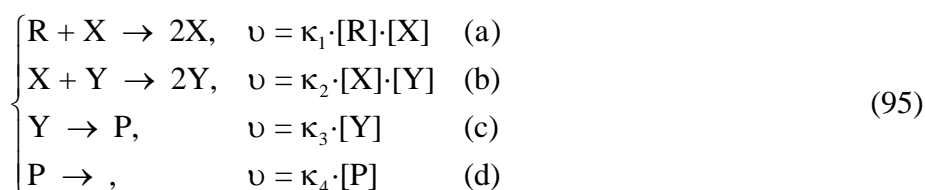


Such as temperature, also the pressure plays an important role in explosions. The 19 figure present the $\log(p)$ – temperature diagram for hydrogen + oxygen mixture. Marked area is the explosion area. The presence of (RS) region is explained by secondary reactions of type (94) facilitating.

11. Lotka – Volterra Autocatalytic Oscillator Model

For the first time Lotka [62] suggested a mechanism of a complex reaction, in homogeneous phase (stage), which shows damped oscillations. Ten years later, in his paper, [63] Lotka modified the mechanism suggested in 1910 in order to generate undamped oscillations.

The mechanism is named Lotka-Volterra and it is further presented. The following pattern of reactions is considered:



The last equation (95d), represents an extraction process of the reaction product P, while the stages (95a) and (95b) are autocatalytic. In L-V model of the reaction mechanism, concentration of the reactant R is maintained constant, (for example either by an addition in the reaction vessel or by an equilibrium between two non-miscible phases when necessary). These restrictions cause the concentrations of X and Y intermediaries/agents to be variable / changeable / unsteady:

$$\dot{[X]} = v_{(29a)} - v_{(29b)} = \kappa_1[\text{R}][\text{X}] - \kappa_2[\text{X}][\text{Y}] \quad (96)$$

$$\dot{[Y]} = v_{(29b)} - v_{(29c)} = \kappa_2[\text{X}][\text{Y}] - \kappa_3[\text{Y}] \quad (97)$$

(96) and (97) equations form a system of differential equations with the functions $[X] = [X](t)$ and $[Y] = [Y](t)$. This system can be simply solved by a numerical method [64]. Thus, the equations (96) and (97) became:

$$x_{n+1} = x_n + (t_{n+1} - t_n) x_n (\kappa_1[\text{R}] - \kappa_2 y_n) \quad (98)$$

$$y_{n+1} = y_n + (t_{n+1} - t_n) y_n (\kappa_2 x_n - \kappa_3) \quad (99)$$

With numerical values:

$$x_0 = [X_0] = 1, y_0 = [Y_0] = 1, \kappa_1 = 3, \kappa_2 = 4, \kappa_3 = 5, [\text{R}] = 2 \quad (100)$$

there can be produced/generated the numerical series/systems $(x_n)_{n \geq 0}$ and $(y_n)_{n \geq 0}$ corresponding to the temporal series $(t_n)_{n \geq 0}$.

In order to obtain an as faithful representation of the mechanism as possible a very fine/careful division of the temporal coordinate in the numerical simulation is required.

Thus, considering the series $t_n = n/10^5$ with $n = 0, 1, \dots, 5 \cdot 10^5$ there are obtained the representations from figs. 20 and 21 for the concentration of the intermediaries $[X] = (x_n)_{n \geq 0}$ and $[Y] = (y_n)_{n \geq 0}$. In the fig. 22 the concentration of the reaction product [P] develops/grows in the time through P_n (the equations 95c and 95d, taking $\kappa_4 = 3$).

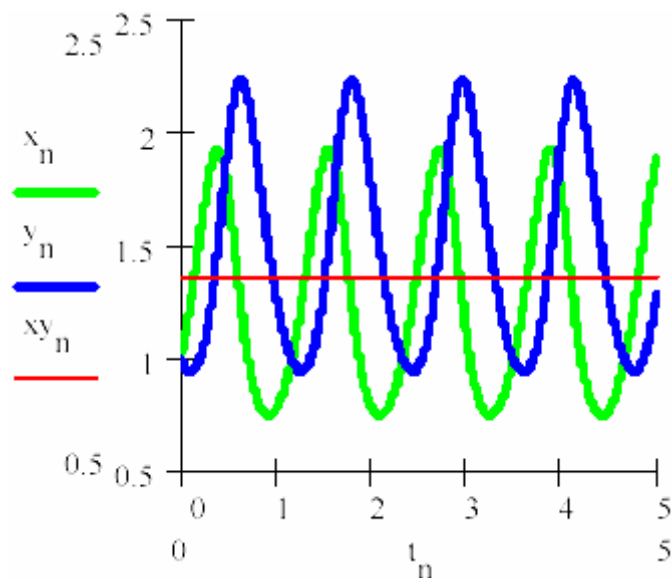


Fig. 20. The oscillation of the intermediaries in L-V mechanism

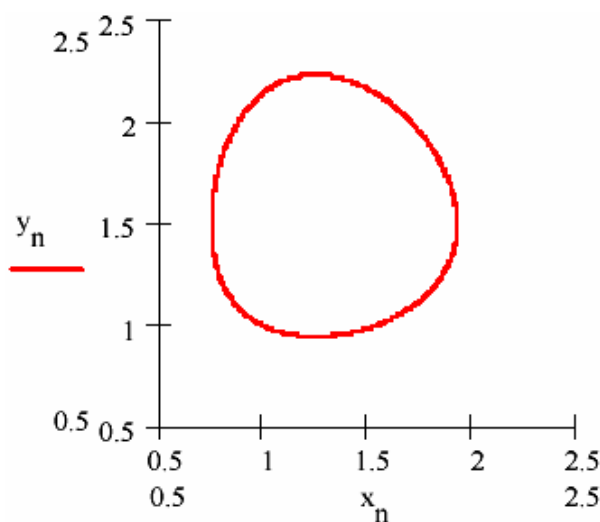


Fig. 21. The variation path ($[X],[Y]$) in L-V mechanism

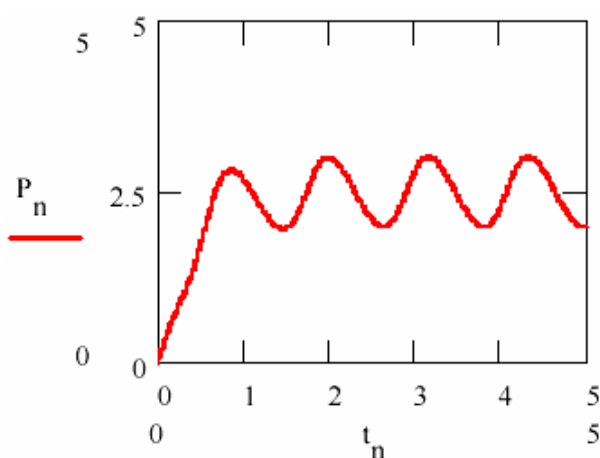


Fig. 22. The variation of the product concentration and storage in L-V mechanism

Carrying out/performing the regression resulted from the equation (95c) and represented in fig. 23, by p_n , according to the concentration $[P]$ and depending on time, the regression slope gives the average rate of formation equal to 1.481.

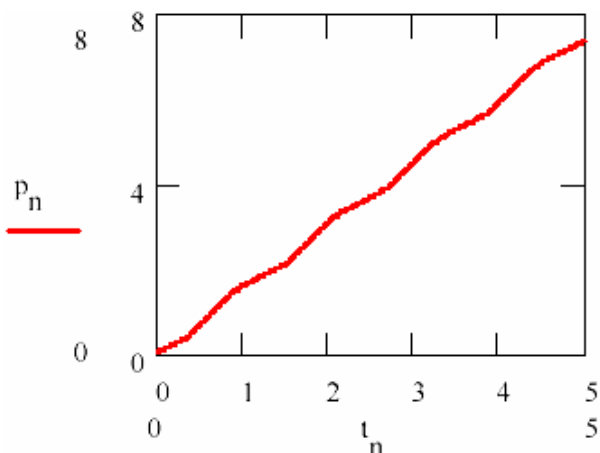
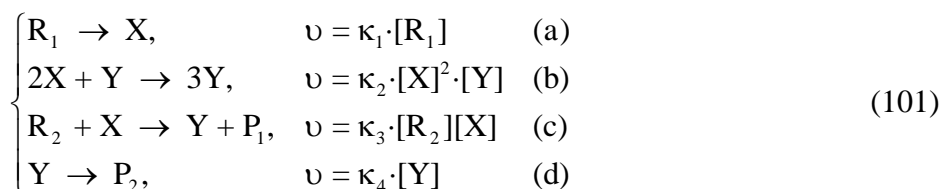


Fig. 23. The variation of the product concentration and storage in L-V mechanism

There are a few remarks to be made, namely: the sum of average concentrations of the agents is maintained in time as the regression equation xy_n also is shows (the slope of the regression equation is null). This average sum $M([X]) + M([Y]) = 1.365$; hence it results that the average concentrations of the agents also remain constant in time; the values of the average concentrations are $M([Y]) = 1.468$ and $M([Y]) = 1.263$.

12. A Model of Damped Oscillations

Let it be a chemical process that takes place according to the following model of a reaction mechanism:



As in Lotka – Volterra, model, the concentrations of the R_1 and R_2 reacting substances remain constant during the process. The solving of the model begins by writing the variation equation for the intermediaries:

$$\dot{[X]} = v_{(34a)} - 2v_{(34b)} - v_{(34c)} = \kappa_1[R_1] - 2\kappa_2[X]^2[Y] - \kappa_3[R_2][X] \quad (102)$$

$$[\dot{Y}] = 2v_{(34b)} + v_{(34c)} - v_{(34d)} = 2\kappa_2[X]^2[Y] + \kappa_3[R_2][X] - \kappa_4[Y] \quad (103)$$

The equations (102) and (103) form a system of differential equations having the functions $[X] = [X](t)$ and $[Y] = [Y](t)$. This system may also be easily solved by a numerical method. The equations (102, 103) are written thus:

$$x_{n+1} = x_n + (t_{n+1} - t_n)(\kappa_1[R_1] - x_n(2\kappa_2x_ny_n + \kappa_3[R_2])) \quad (104)$$

$$y_{n+1} = y_n + (t_{n+1} - t_n)(x_n(2\kappa_2x_ny_n + \kappa_3[R_2]) - \kappa_4y_n) \quad (105)$$

Having the numerical value:

$$x_0 = 0, y_0 = 1, \kappa_1 = 3, \kappa_2 = 4, \kappa_3 = 5, \kappa_4 = 7, [R_1] = 2, [R_2] = 2 \quad (106)$$

there can be generated the numerical series $(x_n)_{n \geq 0}$ and $(y_n)_{n \geq 0}$ corresponding to the temporal series $(t_n)_{n \geq 0}$.

Taking into account the series $t_n = n/100000$ with $n = 0, 1, \dots, 300000$ there are obtained the representation from figs. 24 and 25 for the concentrations of the intermediaries $[X] = (x_n)_{n \geq 0}$ and $[Y] = (y_n)_{n \geq 0}$.

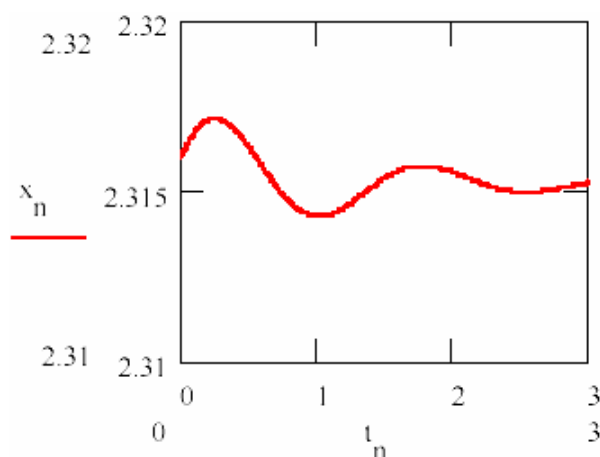


Fig. 24. The damped oscillations in chemical reactions:
the concentration of the intermediary X

Fig. 25 shows that the system tends towards a state of equilibrium state characterized a ratio of the concentrations of the two intermediaries. The system of the agents practically causes damped oscillations around of the equilibrium ratio for two intermediaries. The chart representing the agent concentration $[Y]$ depending on the agent concentration $[X]$ from fig. 26 shows the same thing.

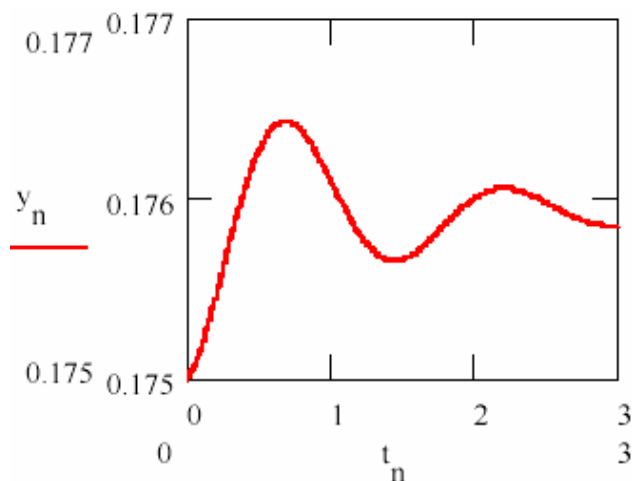


Fig. 25. The damped oscillations in chemical reactions:
the concentration of the intermediary Y

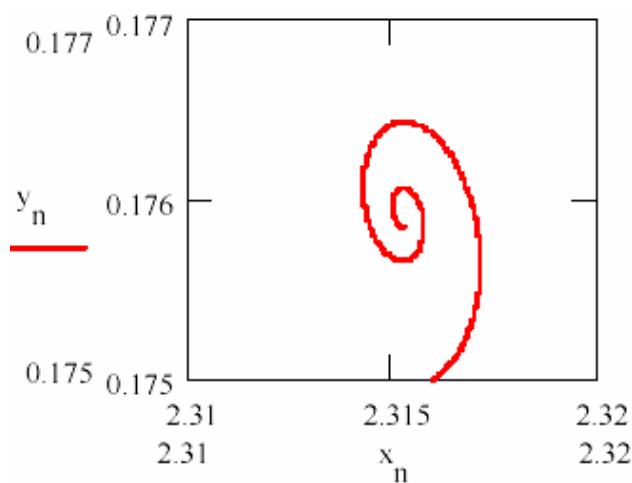


Fig. 26. The damped oscillation path ($[X],[Y]$)

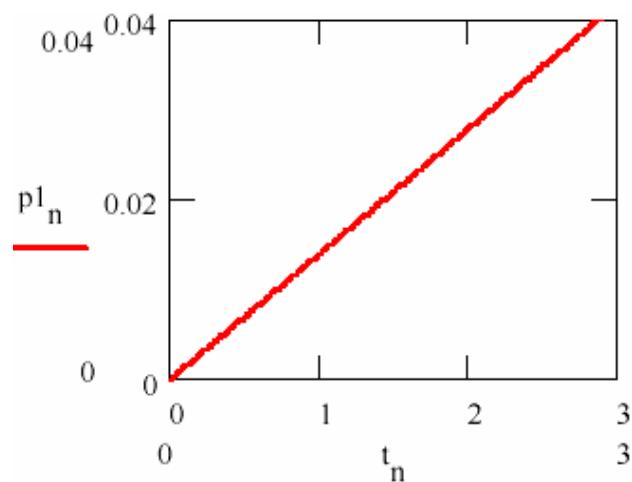


Fig. 27. The linear variation of the amount of products in damped oscillating reactions

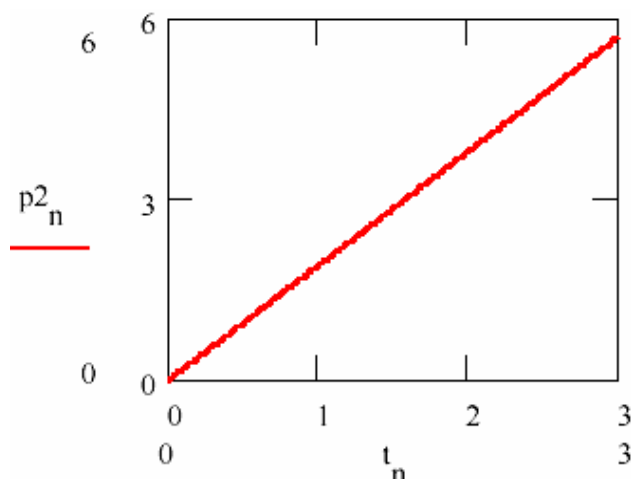


Fig. 28. The linear variation of the amount of products in damped oscillating reactions

The values obtained for the equilibrium concentration are $[X] = 2.315$ and $[Y] = 0.176$ and the equilibrium ratio are $[X]/[Y] = 13.53$.

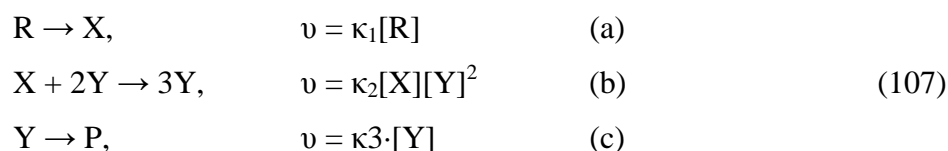
The dependence on time $(t_n)_{n \geq 0}$ of the accumulation of the reaction products $[P1] = (p1_n)_{n \geq 0}$ and $[P2] = (p2_n)_{n \geq 0}$ is given in figs. 27 and 28.

Figs. 27 and 28 shows that this time the concentration of the reaction products changes linearity even if the concentrations of the agents X and Y oscillate towards the equilibrium value.

13. The Brussel Model of Autocatalytic Oscillation

The brussel model was initiated by a group from Bruxelles directed by Ilya Prigogine it introduce for the first time, mechanism of a reaction whose scheme of evolution converged on an attractor [65].

More authors have changed this variant and have studied the systems running according to this mechanism [66, 67]. Further, a simplified variant is presented:



As in the previous situations, it is supposed that the concentration of the reacting substance R remains constant and the product P may be extracted from the system by a reaction of the type (101d).

X and Y are the intermediaries again. Their rate equations written based on the mechanism (107) are:

$$[\dot{X}] = v_{(39a)} - v_{(39b)} = \kappa_1[R_1] - \kappa_2[X][Y]^2 \quad (108)$$

$$[\dot{Y}] = v_{(39b)} - v_{(39c)} = \kappa_2[X][Y]^2 - \kappa_3[Y] \quad (109)$$

Though the equations (108) and (109) seem simpler, at first sight, they are even more difficult to be solved by integration than (96-97) or (102-103). Moreover, the literature has not recorded their integration into the general case described by (108-109).

Besides, the equations (108-109) do not lead to an attractor model not matter by values of the constants of rate and of the concentrations $[R]$, $[X]_0$ and $[Y]_0$. The attempt of solving (108-109) is full of surprises. For most of the values, a system that develops towards a position of equilibrium is obtained; there are values for which damped oscillations to equilibrium are found again; the un-damped periodical oscillations have also an important role, which is confirmed by the majority of the organisms in which the cellular biochemical processes are based on such oscillations.

The processes taking place within the heart are a conclusive example; the periodical heart beats are due to processes of this type. The importance of these processes is great. This was the reason for which Ilya Prigogine was awarded the Nobel Prize for chemistry in 1977, namely for his theories on the dissipative systems.

The equations (108-109) are simplified [68] if $[R] = 1$, $\kappa_1 = 1$ and $\kappa_3 = 1$, are chosen and when the differential system of equations becomes:

$$\dot{x} = 1 - \kappa_2xy^2; \dot{y} = \kappa_2xy^2 - y \quad (110)$$

where the derivate related to the time of the x variable was. This system of the differential equation (110) does not offer more chances for an exact resolution either. However, the numerical simulation is made in the same way. Thus, the iteration equation of variation for (110) is written:

$$x_{n+1} = x_n + (t_{n+1} - t_n)(1 - \kappa_2x_ny_n^2); y_{n+1} = y_n + (t_{n+1} - t_n)(\kappa_2x_ny_n^2 - y_n) \quad (111)$$

Now let us choose $\kappa_2 = 0.88$. Taking into consideration two cases, the first one in which the initial concentrations of the agents are $x_{10} = [X]_{1,0} = 1.5$ and $y_{10} = [Y]_{1,0} = 2$ and second one with $x_{20} = [X]_{2,0} = 2$ and $y_{20} = [Y]_{2,0} = 2.5$. Using the series $t_n = n/100$ with $n = 0, 1, \dots, 150$ following representations for the concentrations of the agents $[X] = (x_n)_{n \geq 0}$ and $[Y] = (y_n)_{n \geq 0}$ are obtained (figures 29 and 30).

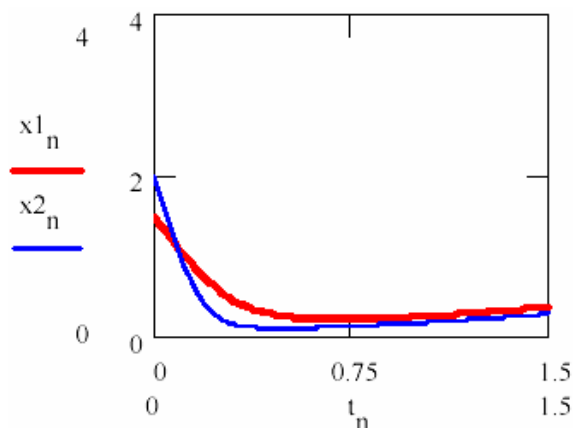


Fig. 29. The concentrations of the X intermediaries up to the attractor for two cases with different initial conditions

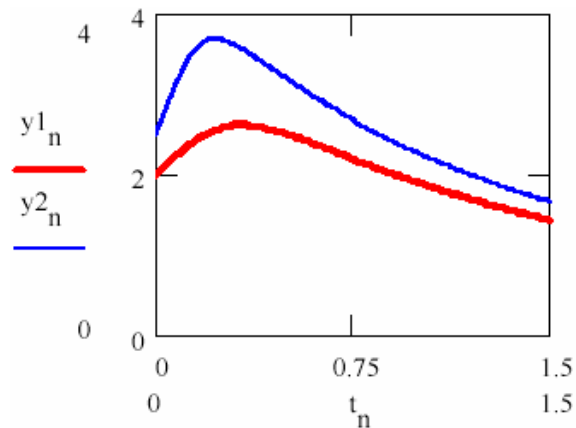


Fig. 30. The concentrations of the Y intermediaries up to the attractor for two cases with different initial conditions

The variation diagram of [Y] depending on [X] and the variation in time of the storage of reaction product are depicted in figure 32.

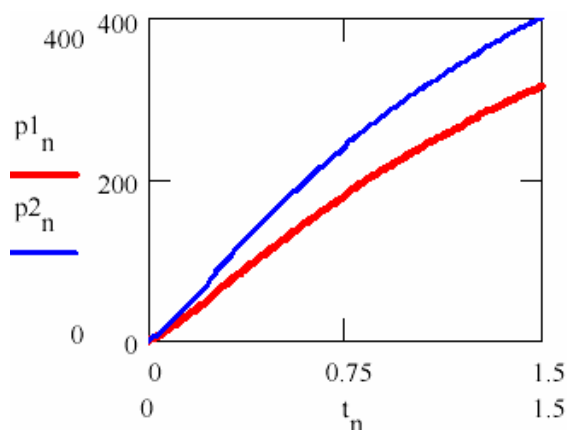


Fig. 31. The product-time dependence in two cases having different initial conditions

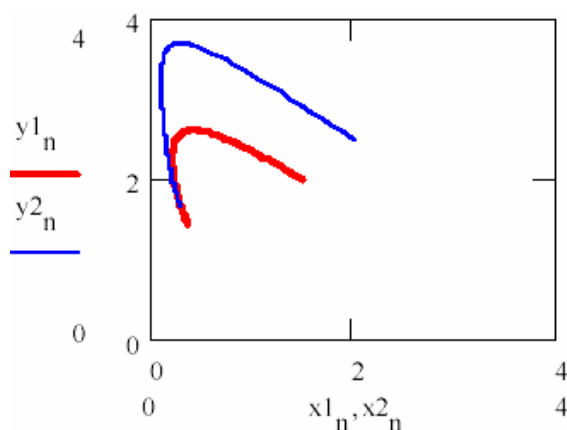


Fig. 32. The ([Y], [X]) hodograph two for cases having different initial conditions

An important observation is that the entrance of [Y] related to [X] on the same gravitational orbit for both cases.

If the figures 29 and 30 are not very conclusive and figure 31 seems to confirm this, fig. 32 shows that, though the two systems start from different values of the concentrations of the agents, in both cases the system comes to evolve rather early on the same trajectory.

Now, increasing the time interval by choosing another $n = 0,1..3000$ the following concentrations of the agents are obtained $[X]_1 = (x1_n)_{n \geq 0}$, $[X]_2 = (x2_n)_{n \geq 0}$, $[Y]_1 = (y1_n)_{n \geq 0}$ and $[Y]_2 = (y2_n)_{n \geq 0}$ for the two cases 1 and 2 of the chosen system (figures 33 and 34). It is noticed that, even if they do not evolve according the same values, same period and amplitude of the oscillations are recorded.

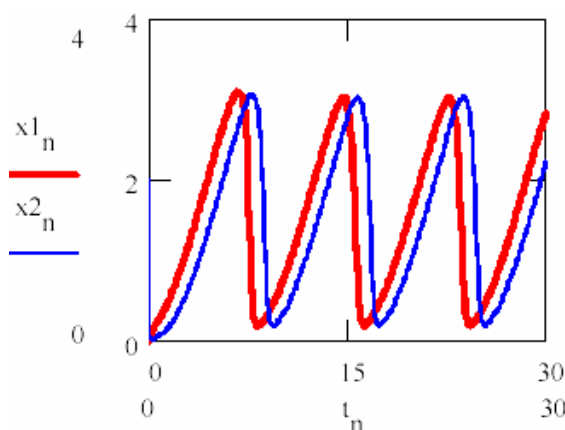


Fig. 33. The periodical evolution having the same different initial conditions
(oscillation period $T = 0.226$ of [X] and [Y])

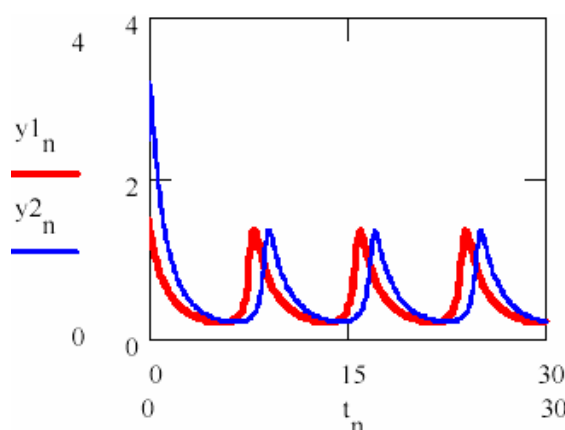


Fig. 34. The periodical evolution having the same different initial conditions
(oscillation period $T = 0.226$ of [X] and [Y])

Fig. 35 gives the dependence of [Y] under [X] for the cases as well as the accumulation of the product.

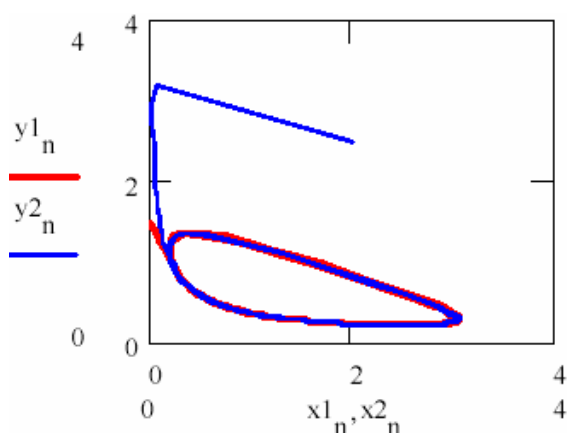


Fig. 35. Convergence at attractor of brusselator system independent from initial conditions

The difference between the Lotka-Volterra model and Bruxelles model one is the following: The Lotka-Volterra model oscillates around the initial values of the concentrations of the agents, whereas the Bruxelles one converges, in time on the same variation equation irrespective of the initial values of the concentrations of the agents. In fact the attractor does not appear for any of their values; for a given k_2 there are minimum $y_{0,\min}$ and $x_{0,\min}$ values from which the periodical oscillations arise and the system tends towards the curve given in fig. 36.

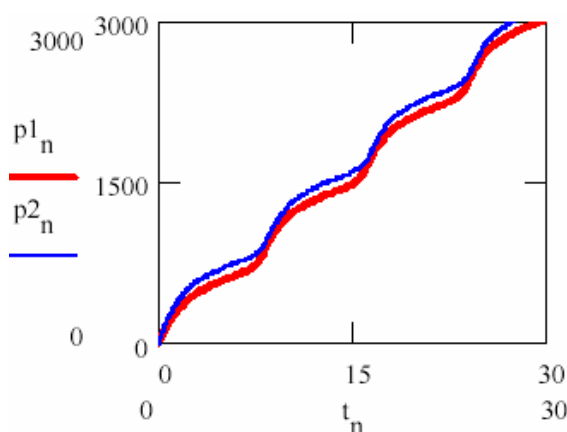


Fig. 36. Different quantities of resulted product for brusselator system

The convergence on the attractor of the brusselator system (a) independent of the initial conditions and (b) different quantities of the product obtained.

Conclusions

There exist a many models of biochemical processes reactions, and every process has some characteristics, as we described below. The importance of every mechanism is given by his applications. It exist much more kinetic models, unexplained in this paper, such as oregonator model [7], one of them implying tens of substances and reactions [69].

As we mentioned before, most spectacular and also important because is most frequent in nature is the brusselator model, every alive organism has one.

The symbolic calculations of reaction rate for biochemical processes are, in most of cases, impossible. In opposite, the numerical modeling of biochemical kinetics proves that it is a very good instrument for mechanism understanding, comparative studies and model validation.

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