# Recording Evolution Supervised by a Genetic Algorithm for Quantitative Structure-Activity Relationship Optimization

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## Abstract

A genetic algorithm for structure-activity relationships optimization was developed and implemented. The genetic algorithm was designed to be feed with families of molecular descriptors, and was tested on Molecular Descriptors Family. The objective of the genetic algorithm was to optimize the multiple linear regressions with four descriptors for prediction of octanol-water partition coefficient (expressed in logarithmic scale) of a series of 206 polychlorinated biphenyls. Relevant factors for evolution were parameterized in the implementation of the evolutionary program. The configuration file allows running of the genetic algorithm under different settings of parameters. The defined parameters were parameters used to characterize the adaptation to the environment (three parameters), to characterize the breading sample (four), the reproduction (four), the evolution objective (two), the selection (ten), the survival (four), and the program execution (three).

**Keywords:** Simulating evolution; Genetic algorithms (GAs); Structure-Activity Relationships (SARs); Multiple Linear Regressions (MLRs).

## Introduction

## Structure-Activity Relationships Optimization

Mathematical approach of SAR (structure-activity relationships) on BAC (biologically active compounds), started in nineteen century and are capitalized through the born of the quantitative structure-activity relationships (QSAR) concept [1], a mathematical tool able to describe the quantitative link between chemical structure and biological activity. SAR records were communicated in scientific literature since 1868, when (first) Crum-Brown & Fraser want to seen if the activity of compounds is or not a function of chemical structure and composition [2]. Only after almost forty years the QSAR paradigm was found useful in agro-chemistry, pharmaceutical chemistry, toxicology, etc [3]. Scientific literature contains many reports on usage of QSARs in the methodology of designing new BACs (the monograph [4] covers a good part of them).

#### Evolution Supervised by Genetic Algorithms

Hard [5] and soft [6] inheritance, selection and survival [7], traits [8] and genes [9] crossover, a long and contentious debate over the 19th century [10] are all pieces from a puzzle build today the modern genetics [11] and were the sources of inspiration for genetic algorithms (GAs).

First studies on simulating an evolution were published by Nils Aall BARRICELLI [12]. Alex FRASER (1923-2002) also published a series of studies about simulation of artificial selection of organisms having multiple loci controlling a measurable trait. Fraser's simulations [13-25] included all essential elements of modern GAs.

## Recording Evolution Supervised by a Genetic Algorithm

The research question "How the evolution can be observed and characterized via different parameters characterizing the sample supervised to evolutes?" are not enough explored in the specialty literature on genetic algorithms subject. Studies of different operators essential for evolution are focused mainly on algorithm efficiency and a representative manuscript for this approach is the collection from [26].

A small number of studies described the influence of the evolution strategy on evolution objective and almost nothing about the influence of different parameters characterizing the evolving sample on evolution objective.

The GAs passed out the border of the informatics field a long time ago, because of their results capitalization potential. PhD theses that had as objectives project, implement and use of genetic algorithms are found practically in all fields of research. Thus, in agriculture GAs were found useful to crop planning [27], in constructions to assess the risk of soil damage [28], in bioengineering to efficient control of pollution at a hydrographic basin level [29], in chemistry at design of sensorbased controlled processes [30], in economics at optimization of problems with multiple options [31], in management at multi-scale processes modeling [32], in mechanics at optimization of composite structures [33], in environment at strategy chousing for water quality control [34], in biology in phylogenetic analysis [35] and evolution studies [36].

#### Research Aim of the Paper

The research aim to project a GA and to implement it as an evolutionary program, capable to record the influence of different samples, environments and intrinsic parameters of genetic algorithm on evolution supervised by the genetic algorithm feed with data for structure-activity relationships optimization in a series of biologically active compounds.

#### Material and Method

#### Material

The chosen set of molecules for the study is

The PCBs data set (with 209 compounds in the series) was the set of compounds choused for this study. The log(Kow) was the available data measured in same experimental conditions for 206 compounds [37-39].

HyperChem (licence v. 8.0/2007) was used for drawing and optimizing the compounds (using AMBER molecular mechanics model, POLAK-RIBIERE optimization algorithm, and AM1 method for semiempirical energy calculations). Molecular Descriptors Family [40-42] was used to create the population of structural descriptors that feed the genetic algorithm. The search was started for multiple linear regressions with four descriptors members of MDF relating the observed log(Kow) of 206 PCBs. Grubbs test [43] was used to identify outliers (PCB209) in the experimental; data.

### Method: Search Space and Genetic Algorithm

Every gene codifies an operator used in construction of the chromosome of a molecular descriptor. Every descriptor (of a family of descriptors, such as MDF) is a genotype and all together is the genetic material of the family. Table 1 presents the search space created for MDF.

| Family | Gene           | G | eno | me |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   | <br> |  |  |
|--------|----------------|---|-----|----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|------|--|--|
| MDF    | D <sub>M</sub> | t | g   |    |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |      |  |  |
|        | Ap             | С | Н   | Μ  | Е | G | Q |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |      |  |  |
|        | ID             | D | d   | Ο  | 0 | Р | р | Q | q | J | j | Κ | k | L | 1 | V | Е | W | w | F | f | S | s | Т | t |      |  |  |
|        | $I_{M}$        | r | R   | m  | Μ | d | D |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |      |  |  |
|        | F <sub>C</sub> | m | Μ   | D  | Р |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |      |  |  |
|        | SM             | m | М   | n  | Ν | S | А | а | В | b | Р | G | g | F | f | s | Η | h | Ι | i |   |   |   |   |   |      |  |  |
|        | Lo             | Ι | i   | А  | а | L | 1 |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |      |  |  |

Table 1. MDF search space

The working methodology of genetic algorithms suppose a initial prelevation (at random or using a strategy) of a *sample* of chromosomes from the genetic material - in this case a array of MDF members from  $X_1$  to  $X_p$  which enters in *cultivar* for conducting the *evolution process*. The *genetic algorithm* operates on the sample which is changed (in part) in every generation. Every set of `n` descriptors (where n is the multiplicity order for MLR) is a point in the *search space* and a *possible solution*. The operators which change the genetic code are crossover and mutated. Crossover of two genotypes suppose chousing of a part from the stream of genes to be crossover (at random or using a strategy) and the values of the parts are switched one in the place of the other, and two descendents are produced. Mutation of a genotype supposes the changing of the value of a (or more) gene with other allowed value from the list of possible values for a given gene. Both crossover and mutation produces *descendents*. The *selection* of the genotypes is the operation which mutation and crossover calls for, are based on a *strategy* and uses a score function (*selection score*). At least a part of the descendents are *viable* (descriptors), being able to be part of a viable solution (MLR) in the next generation(s). Viable descriptors replace a part from the sample through a *survival* process. As selection process, survival process uses a score function (*survival* score) and uses a strategy. The evolution objective are recorded during evolution using a score function (objective score). The individuals which gives the best objective score in every generation (enters in the best MLR) are marked. The marked individuals are automatically qualified for the next generation (no survival strategy applies on it). Not all individuals of a generation (including parents and descendants) survive and will be part of the next generation. This is done in order to keep constant the sample size (thus the number of replaced individuals is equal to the number of viable descendants).

Selection and survival based on selection and survival scores are applied through selection and survival strategies, using an *algorithm*. *PS* algorithm constructs a *proportional strategy* using an array of scores and gives to an individual a chance (to be selected in selection process or to be killed in survival process) proportional with the score; it returns a given number N\_Sel of individuals using their chances. *DS* algorithm constructs a *deterministic strategy* returning the N\_Sel individuals with the first N\_Sel highest scores (applies a random qualification at equal scores if it is necessary). *TS* algorithm constructs a *tournament strategy* using the array of scores and qualifies N\_Sel individuals through a repeated N\_Sel times tournament of two individuals.

The genetic algorithm acts as follows:

- The sample of the given size (N\_Gen) is created (it contains predefined or random individuals);
- Repeat steps 1..6 until objective score is satisfactory or a number of generations are exhausted;
- Step\_1: Computes selection, survival and objective scores (and eventually include in the next generation the marked individuals);
- Step\_2: Select N\_Cro pairs of individuals (using selection strategy);
- Step\_3: For every one from 2×N\_Cro, using p\_Par (low) probability and a discrete uniform distribution pick up a number of N\_Mut genes and make a mutation on it (parents); save the result

(whatever mutated or not, 2×N\_Cro individuals);

- Step 4: For every one from N\_Cro, using a discrete uniform distribution pick up the sequence of genes to be crossover, perform the crossover and save the results (replace the previous one, 2×N\_Cro individuals);
- Step\_5: For every one from 2×N\_Cro, using p\_Chi (low) probability and a discrete uniform distribution pick up a number of N\_Mut genes and make a mutation on it (child); save the results (whatever mutated or not; replace the previous one, 2×N\_Cro individuals);
- Step\_6: Replace (using the survival strategy) a part of N\_Gen with a part of 2×N\_Cro;

## **Results and Discussion**

A series of parameters influence the evolution and should be taken into account when a genetic algorithm is implemented. Table 2 presents a list of parameters that proved to be relevant.

| Class        | Parameter                       | Type (and values for lists)                         |  |  |  |  |  |  |
|--------------|---------------------------------|---|--|--|--|--|--|--|
| Adaptation   | a_v_ADAPT_Variance              | Real  |  |  |  |  |  |  |
|              | ajb_ADAPT_JarqueBera            | Real  |  |  |  |  |  |  |
|              | a_c_ADAPT_Correlation           | Real  |  |  |  |  |  |  |
| Sample       | sn0_SAMPLE_Size                 | Integer (natural)                                   |  |  |  |  |  |  |
|              | rn0_REGRESSION_Multiple         | Integer (natural)                                   |  |  |  |  |  |  |
|              | e1n_GENERATIONS_max             | Integer (natural)                                   |  |  |  |  |  |  |
|              | g_r_GENERATIONS_first_rich      | List: {Yes, No}                                     |  |  |  |  |  |  |
| Reproduction | cn0_CROSSOVER_Pairs             | Integer (natural)                                   |  |  |  |  |  |  |
|              | m_m_MUTATION_Genes              | Integer (natural)                                   |  |  |  |  |  |  |
|              | mpp_MUTATION_Parent_probability | Real  |  |  |  |  |  |  |
|              | mcp_MUTATION_Child_probability  | Real  |  |  |  |  |  |  |
| Evolution    | b_p_EVOLUTION_parameter         | List: {r2, se, Mt, Hr}                              |  |  |  |  |  |  |
|              | b_o_EVOLUTION_objective         | List: {min, max}                                    |  |  |  |  |  |  |
| Selection    | sfs_SELECTION_strategy          | List: {proportional, deterministic, tournament}     |  |  |  |  |  |  |
|              | sfn_SELECTION_normalized        | List: {Yes, No}                                     |  |  |  |  |  |  |
|              | sfr_SELECTION_ranks             | List: {Yes, No}                                     |  |  |  |  |  |  |
|              | sfa_SELECTION_accuracy          | Integer (natural)                                   |  |  |  |  |  |  |
|              | sff_SELECTION_function          | List: {nalive, r2_min, se_min, Mt_min, Hr_min,      |  |  |  |  |  |  |
|              |                                 | r2_max, se_max, Mt_max, Hr_max, r2_avg,             |  |  |  |  |  |  |
|              |                                 | se_avg, Mt_avg, Hr_avg}                             |  |  |  |  |  |  |
|              | sfo_SELECTION_objective         | {min, max}  |  |  |  |  |  |  |
|              | fr2_SELECTION_r2_p              | Real  |  |  |  |  |  |  |
|              | fse_SELECTION_se_p              | Real  |  |  |  |  |  |  |
|              | fMt_SELCTION_Mt_p               | Real  |  |  |  |  |  |  |
|              | fHr_SELECTION_Hr_p              | Real  |  |  |  |  |  |  |
| Survival     | v_p_SURVIVAL_phenotyping_p      | Real  |  |  |  |  |  |  |
|              | v_g_SURVIVALgenotyping_p        | Real  |  |  |  |  |  |  |
|              | vfs_SURVIVAL_strategy           | List: {proportional, deterministic, tournament}     |  |  |  |  |  |  |
|              | vfr_SURVIVAL_ranks              | List: {Yes, No}                                     |  |  |  |  |  |  |
| Execution    | e0n_RUNS_number                 | Integer (natural)                                   |  |  |  |  |  |  |
|              | b_k_RUNS_kepp_best_in_sample    | List: {Yes, No}                                     |  |  |  |  |  |  |
|              | b_f_RUNS_get_best_from_file     | List: {Yes, No} + list of genotypes in a file named |  |  |  |  |  |  |
|              |                                 | c_galg.txt  |  |  |  |  |  |  |

Table 2. Configuration of the evolution: classes and parameters

 Adaptation parameters - in a series of three - refers the environment of the evolution in terms of viability of the phenotypes in the environment; these parameters defines limits - Variance and Correlation defines minimal values, JarqueBera defines maximal value - required to phenotypes to be considered alive in the environment.

- Sample parameters in a series of four refer the sample and their cultivar Sample Size is the 'room' in the environment reserved for breeding; Regression Multiple is the number of phenotypes which participates as independent variables in the MLR; Generations Max is the maximum number of generations in which the GA is run in the process of MLR optimization; Generations First Rich is a choice to repeat the random selection of the initial generation genotypes until all genotypes has at least one alive phenotype in the environment.
- Reproduction parameters in a series of four defines the way in which reproduction are made in a
  generation; Crossover Pairs is the number of pairs of genotypes which are crossover; Mutation
  Genes is the number of genes which are mutated when mutation occurs; Mutation Parent
  Probability controls when mutation occurs before crossover (at parents) and Mutation Child
  Probability controls when mutation occurs after crossover (at child).
- *Evolution parameters* two parameters define the objective function (Evolution Parameter) and its objective (Evolution Objective).
- Selection parameters in a series of 10 defines the strategy of selection (Selection Strategy), if the values are normalized between generations (Selection Normalized), if are used their ranks in place of their values (Selection Ranks), an integer defining a factor with which the selection scores is multiplied and rounded to integers (to create a discrete space of probabilities from scores required especially for Proportional Selection), a series of alternatives for selection function (Selection Function), the objective of a given alternative (Selection Objective), a power at which the result of the function to be rising up rescales the values in terms of probabilities of selection (here four values should be specified, but just one gives the expression used at selection function this one correspond to the defined alternative).
- Survival parameters in a series of four defines the strategy for replacing the genotypes (Survival Strategy), if are used ranks in places of values of the survival function (Survival Ranks) and two parameters defining the weight of the genotype similarity (Survival Genotyping) and phenotype similarity (Survival Phenotyping) in the expression of the global similarity score of two individuals.
- Execution parameters in a series of thee define the behavior in execution of the evolutionary program; Runs Number is the number of independent runs of the genetic algorithm restarting the search from a initial generation; Runs Keep Best In Sample defines if genotypes giving best MLR model in a generation enters in the survival process or are directly qualified for the next generation; Runs Get Best From File are a option useful for repeated optimization procedures in order to improve a previous obtained MLR.

Table 3 shows the parameters which were used in the optimization of a MLR with four MDF descriptors acting as QSAR on log K<sub>ow</sub> of a series of 206 PCBs.

Only a part of the genotypes from the entire population were adapted to the environment the rules for viability defined by the values from Table 3 were applied. Thus, almost 46% (60337/131328) of the genotypes provided at least one adapted phenotype. About 20% ( $26355 \times 26324/131328$ ) of the phenotypes created by *Identity* and *Absolute* linearization operators (first and respectively third entries in Genome at L<sub>0</sub> gene in Table 1), almost 18% (24085) of *logarithm* (1) entry in same table), and almost 23% of *Logarithm* of absolute ('L' entry, 29973 adapted phenotypes), *inverse* ('i', 30178) and *absolute* inversed ('a', 30174) were adapted.

The average value of the determination coefficients obtained in 46 runs (Table 3) for nine pairs of selection and survival strategies (Table 5) was of 0.8808 (414 observations) with a range between 0.8804 and 0.8811 at a 5% risk of being in error.

The evolution was observed in first generation in 28.5% (118/414) of the cases when the determination was improved to 0.8816 ranging between 0.8810 and 0.8823 at a 5% risk of being in error. The determination coefficient obtained after evolution in first generation was statistically significant different from the determination coefficient obtained in the first generation (the risk of being in error was about 3%) without costs in variability (F ratio comparing variances is 1.1, probability to observe at random such event is 52%).

A list of parameters used to set up the output was defined (Table 4) in order to have detailed observation of the evolution.

| Parameter                       | Value  |  |  |
|---------------------------------|--------|--|--|
| a_v_ADAPT_Variance              | 0.1    |  |  |
| ajb_ADAPT_JarqueBera            | 1.0    |  |  |
| a_c_ADAPT_Correlation           | 0.1    |  |  |
| sn0_SAMPLE_Size                 | 12     |  |  |
| m0_REGRESSION_Multiple          | 4      |  |  |
| e1n_GENERATIONS_max             | 20000  |  |  |
| g_r_GENERATIONS_first_rich      | Yes    |  |  |
| cn0_CROSSOVER_Pairs             | 2      |  |  |
| m_m_MUTATION_Genes              | 2      |  |  |
| mpp_MUTATION_Parent_probability | 5%     |  |  |
| mcp_MUTATION_Child_probability  | 5%     |  |  |
| b_p_SELECTION_parameter         | r2     |  |  |
| b_o_SELECTION_objective         | max    |  |  |
| sfn_FITNESS_normalized          | No     |  |  |
| sfr_FITNESS_ranks               | No     |  |  |
| sfa_FITNESS_accuracy            | 10000  |  |  |
| sff_FITTEST_function            | r2_min |  |  |
| sfo_FITTEST_objective           | max    |  |  |
| fr2_FITTEST_r2_p                | 1.0    |  |  |
| fse_FITTEST_se_p                | 1.0    |  |  |
| fMt_FITTEST_Mt_p                | 1.0    |  |  |
| fHr_FITTEST_Hr_p                | 1.0    |  |  |
| v_p_SURVIVAL_phenotyping_p      | 1.0    |  |  |
| v_g_SURVIVALgenotyping_p        | 1.0    |  |  |
| vfr_SURVIVAL_ranks              | No     |  |  |
| e0n_RUNS_number                 | 46     |  |  |
| b_k_RUNS_kepp_best_in_sample    | Yes    |  |  |
| b_f_RUNS_get_best_from_file     | No     |  |  |

Table 3. Configuration of the evolution

Table 4. Configuring the output

| Parameter   | Value  |  |  |
|---|--------|--|--|
| d_d_SHOW_descriptive_XX   | Yes/No |  |  |
| (XX = m0, m1, m2, m3, m4, mx, my, v0, g1, g2, jb, r1, r2)             |        |  |  |
| d_f_SHOW_fitness_YY   | Yes/No |  |  |
| (YY = nalive, r2_min, se_min, Mt_min, Hr_min, r2_max, se_max, Mt_max, |        |  |  |
| Hr_max, r2_avg, se_avg, Mt_avg, Hr_avg)                               |        |  |  |
| d_s_SHOW_genotypes  | No/Yes |  |  |
| d_p_SHOW_phenotypes   | No/Yes |  |  |
| d_m_SHOW_mols   | No/Yes |  |  |
| d_g_SHOW_generations  | No/Yes |  |  |
| d_e_SHOW_evolutions   | Yes/No |  |  |
| d_c_SHOW_configuration  | Yes/No |  |  |

Table 5. Selection and survival strategies in genetic algorithms: run results

| Selection     | Survival      | Configuration    | Evolution               |  |  |  |  |  |
|---------------|---------------|------------------|-------------------------|--|--|--|--|--|
| Proportional  | Proportional  | PCB 4044 cfg.txt | PCB 4044 evo.txt        |  |  |  |  |  |
| Proportional  | Deterministic | PCB 2441 cfg.txt | PCB 2441 evo.txt        |  |  |  |  |  |
| Proportional  | Tournament    | PCB 9878 cfg.txt | PCB 9878 cfg.txt        |  |  |  |  |  |
| Deterministic | Proportional  | PCB 5108 cfg.txt | PCB 5108 evo.txt        |  |  |  |  |  |
| Deterministic | Deterministic | PCB 6369 cfg.txt | PCB 6369 evo.txt        |  |  |  |  |  |
| Deterministic | Tournament    | PCB_6690_cfg.txt | <u>PCB_6690_evo.txt</u> |  |  |  |  |  |
| Tournament    | Proportional  | PCB 5828 cfg.txt | PCB 5828 evo.txt        |  |  |  |  |  |
| Tournament    | Deterministic | PCB 4872 cfg.txt | PCB 4872 evo.txt        |  |  |  |  |  |
| Tournament    | Tournament    | PCB_1758_cfg.txt | PCB_1758_evo.txt        |  |  |  |  |  |

The parameters from Table 4 allow the user to configure its output including or excluding some of them. The meanings of the parameters are as follows:

- The generic parameters d\_d\_SHOW\_descriptive\_XX and d\_f\_SHOW\_fitness\_YY are lists (XX = m0, m1, m2, m3, m4, mx, my, v0, g1, g2, jb, r1, r2; YY = nalive, r2\_min, se\_min, Mt\_min, Hr\_min, r2\_max, se\_max, Mt\_max, Hr\_max, r2\_avg, se\_avg, Mt\_avg, Hr\_avg), every item in the list defining an observable (and <u>Supplementary Material (online)</u>);
- d\_s\_SHOW\_genotypes add a number of columns equal with sample size and containing the genotypes which gives at least an adapted phenotype;
- d\_p\_SHOW\_phenotypes add six times of sample size columns in the output file containing the adapted phenotypes;
- d\_m\_SHOW\_mols add extra columns in `\_cfg.txt`, `\_evo.txt`, and `\_gen.txt` output files containing the predictions based on the best available MLR;
- d\_g\_SHOW\_genarations set to Yes produces the `\_gen.txt` file containing one row per generation;
- d\_e\_SHOW\_evolution set to Yes produces the `\_cfg.txt` file containing only the results when an evolution occurs;
- d\_c\_SHOW\_configuration set to Yes produces the `\_cfg.txt` file containing only the results after entire cycles of evolution;

The created evolutionary program was used to show the influence of different selection and survival strategies on evolution supervised by the genetic algorithm when was feed with data for structure-activity relationships optimization in the PCB series of biologically active compounds were recorded.

Two parameters (*sfs\_FITNESS\_strategy* and *vfs\_SURVIVAL\_strategy* - see Table 2) took different values once at the time for the parameters kept constant (the above table), nine executions of the program were independently started, and the results were recorded in separate files (two files per execution, Table 4).

The following information was available in the *PCB\_XXX\_evo.txt* files:

- e1i: generation (integer) in which a new evolution occurred (evolution refers the value of the objective function r2 → max.; evolution meant the obtaining of a QSAR with a determination coefficient higher than the one previously obtained);
- sn2: number of viable genotypes (not always all genotypes from crossovers and mutations are viable has at least one adapted phenotype; maximum number of viable genotypes is the sample size sn0 see Table 2);
- pn2: number of adapted phenotypes; maximum number of adapted phenotypes is six times of sn2);
- nrali: number of phenotypes associations (regressions) obtained with individuals from cultivar of the sample; phenotypes associations are obtained combining rn0 - see Table 2 - distinct phenotypes and the same adaptation requirements are for the association as are the requirements for a phenotype;
- Gen11..Gen0: the genotype in position from 12 down to 1 in the places of the sample in a given moment of evolution;
- rr2: value of the objective function of evolution (see Table 3); the determination coefficient of the best available SAR expressed as MLR with 4 MDF descriptors existing in the sample;
- rse: the value of the (alternative) objective function "estimation errors sum";
- rMt: the value of the (alternative) objective function "mean of Student t values of the regression parameters";
- rHr: the value of the (alternative) objective function "the entropy of the determination";
- rdr: number of coefficients in the MLR giving the best available MLR; rdr=rn0+1 if the free term are present (is not null at 5% risk being in error) and rdr=rn0 otherwise;
- rme: mean squared error (MSE) of the regression that provided the best available MLR;
- rdt: number of degrees of freedom in the best available MLR (nmo rdr);
- rm0: the absolute value of the mean of estimate,  $M(|\hat{Y}|)$ ;
- rm1: mean of the estimate,  $M(\hat{Y})$ ;
- rm2: the mean  $M((Y-\hat{Y})^2)$ ;
- rm3: the mean M((Y-Ŷ)<sup>3</sup>);
- rm4: the mean  $M((Y-\hat{Y})^4)$ ;

- rmx: the mean  $M(\hat{Y}^2)$ ;
- rmy: the mean M(YŶ);
- rv0: rm2/rm0<sup>2</sup>;
- rg1: skewness (g1) of the estimated (Ŷ);
- rg2: kurtosis excess (g2) of the estimated (Ŷ);
- rjb: the Jarque-Bera (JB) statistic of the estimated (Ŷ);
- rr1: r(Y,Ŷ);
- rr2:  $r^{2}(Y, \hat{Y});$
- malive: 0 (when  $\hat{Y}$  are not adapted) or 1 (when  $\hat{Y}$  are adapted);
- rr2\_min: value "r2\_min" of the selection score FS; are given by Ŷ to the phenotypes from which are composed (min, max and avg are identical here, referring the min, average and max from a single value); rse\_min: value of the alternative "se\_min" of the selection score FS; rMt\_min: value of the alternative "Mt\_min" of the selection score FS; rHr\_min: value of the alternative "Hr\_min" of the selection score FS; rHr\_min: value of the se
- rr2\_max: idem rr2\_min; rse\_max: idem rse\_min; rMt\_max: idem rMt\_min; rHr\_max: idem rHr\_min; rr2\_avg: idem rr2\_min; rse\_avg: idem rse\_min; rMt\_avg: idem rMt\_min; rHr\_avg: idem rHr\_min;
- gnalive: in the generations which produces evolution (and only these are listed in this file and in the defined configuration of the execution) are identical with nrali; nrali keeps the number of obtained regressions with individuals from last (including the current) generation producing evolution and gnalive refers the current generation (without regarding to evolution);
- gr2\_min: value "r2\_min" of selection score FS given by the descriptors existing in sample in the generation; gse\_min: value of "se\_min" alternative; gMt\_min: value of "Mt\_min" alternative;
- gHr\_min: value of "Hr\_min" alternative; gr2\_max: value of "r2\_max" alternative; gse\_max: value of "se\_max" alternative; gMt\_max: value of "Mt\_max" alternative; gHr\_max: value of "Hr\_max" alternative; gr2\_avg: value of "r2\_avg" alternative; gse\_avg: value of "se\_avg" alternative; gMt\_avg: value of "Mt\_avg" alternative; gHr\_avg: value of "Hr\_avg" alternative;
- regression\_equation: best MLR obtained with descriptors with the genotype in the sample;
- The following information was available in the *PCB\_XXX\_dg.txt* files:
- Configuration part:
  - o My\_Data=172.27.211.5/MDFSARs[PCB\_lkow\_data;PCB\_lkow\_tmpx] IP of the server, database, tables with input data;
  - Genomes=Genes:[mp;fc;oi;id;ap;dm]/Addre:[fc;ap;id;oi;dm;mp] definition of the genome and the calculation of the address in the table (a permutation of the definition, used to access fast the data in the `\_tmpx` table);
  - G\_Codes=mMnNSPsAaBbGgFfHhIi/mMDP/RrMmDd/DdOoPpQqJjKkLIVEWw FfSsTt/CHMEGQ/gt - list of the codes for every gene of the genome;
  - N\_Sizes=Sample:12/CrossO:2/RegreM:4/MutGen:2 sample size; number of crossovers; number of descriptors in MLR; number of genes to be mutated when mutation occurs;
  - Adapted=AbsVariance: 1.6353599751539131E-0003(0.100)/Jarque-Bera: 7.5766145463847375E+0000(1.000)/Determinate:0.100(%)/StudentTVal:[ 1.9721423227715891E+0000(201); 1.9720824746250930E+0000(202)] v0 (correspondent of rv0 din PCB\_XXXX\_evo.txt for the observed (Y); jb (correspondent of rjb din <u>PCB\_XXXX\_evo.txt</u> for the observed (Y); lowest determination coefficient to be adapted; Student t from Student distribution corresponding to a model of regression with free term (df=nmol-RegM-1) and without free term (df=nmol-RegM) used as limits in the two cases to accept or reject the model;
  - Mutated=ParentsProb:0.050/ChildreProb:0.050 probability (in percents) to occur mutation before crossover (parents are then mutated); probability (in percents) to occur mutation after crossover (children are then mutated);
  - Objectiv=Parameter:r2/To:max the name of the objective function chosed to be used in the evolution process; the objective of the objective function;

- Selected=Parameter:r2\_min/To:max/Using:tournament/Normalized?:No/SortedRank?
   :No/First\_Rich?:Yes which is the observable in selection; which is the selection objective; which is the strategy of selection; if the strategy is applied on normalized (between generations) values; if ranks replaces the values when the strategy are applied; first generation is rich in adapted genotypes (all adapted) or not;
- Survival=Phenotyping:1.000/Genotyping:1.000/Using:tournament/SortedRank?:No the value of the weight of the phenotypic similarity in the survival score; the value of the weight of the genotypic similarity in the survival score; the strategy of the survival; if ranks replaces the values when the strategy are applied;
- Evolution=nalive;r2\_min;se\_min;Mt\_min;Hr\_min;r2\_max;se\_max;Mt\_max;Hr\_max;r2 \_avg;se\_avg;Mt\_avg;Hr\_avg; - parameters recorded during evolution;
- Alive=Genotypes:60337/Phenotypes(I):26355;/Phenotypes(A):26324;/Phenotypes(I):24 085;/Phenotypes(L):29973;/Phenotypes(i):30178;/Phenotypes(a):30174; total number of adapted in the entire population: genotypes, and phenotypes by linearization operator (see Table 1);
- Repeated=Sampling:45 number of repetitions is one unit more (here are the lower limit for construction of a statistical significance);
- Repetition: number of repetition in the independent run of the GA starting from a random initial sample;
- Found: number of the generation in current repetition when a evolution occurred;
- All other parameters corresponds to the same ones from PCB\_XXXX\_evo.txt file: r2=rr2, se=rse, Mt=rMt, Hr=rHr, dr=rdr, me=rme, dt=rdt, m0=rm0, m1=rm1, m2=rm2, m3=rm3, m4=rm4, mx=rmx, my=rmy, v0=rv0, g1=rg1, g2=rg2, jb=rjb, r1=rr1, r2=rr2, nalive=rnalive, r2\_min=rr2\_min, se\_min=rse\_min, Mt\_min=rMt\_min, Hr\_min=rHr\_min, r2\_max=rr2\_max, se\_max=rse\_max, Mt\_max=rMt\_max, Hr\_max=rHr\_max, r2\_avg=rr2\_avg, se\_avg=rse\_avg, Mt\_avg=rMt\_avg, Hr\_avg=rHr\_avg, regression\_equation= regression\_equation).

## Conclusions

A genetic algorithm for identification the most close to the optimum multiple linear regression models was developed and implemented to be use in identification of quantitative structure-activity relationship models. The genetic algorithm was designed to be feed with families of molecular descriptors, and was tested on the Molecular Descriptors Family.

The objective of the genetic algorithm was to optimize the multiple linear regressions with four descriptors for prediction of octanol-water partition coefficient (expressed in logarithmic scale) of a series of 206 polychlorinated biphenyls and was successfully accomplished.

The average of the determination coefficients obtained in 46 runs for nine pairs of selection and survival strategies was of 0.8808 (414 observations) with a range between 0.8804 and 0.8811 (at a risk to be in error of 5%).

The evolution was observed in first generation in 28.5% (118/414) of the cases when the determination was improved to 0.8816 (with a range from 0.8810 to 0.8823, at a 5% risk to be in error). The determination coefficient obtained after evolution in first generation proved to be statistically significant different from the determination coefficient obtained in the initial generation (for a level of significance of 3%) without costs in variability (F ratio comparing variances was 1.1, probability to observe at random such event being 52%).

## **Conflict of Interest**

The author declares that they have no conflict of interest.

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